

## MINNESOTA TIMSS: The Rest of the Story

A SUMMARY OF RESULTS AS OF OCTOBER 2009

TRENDS IN INTERNATIONAL MATHEMATICS AND SCIENCE STUDY

### MINNESOTA SCIENCE AND MATH COMPARED INTERNATIONALLY IN TIMSS: REVIEWING THE CONTEXT

The 2007 TIMSS is referred to as the Trends in International Mathematics and Science Study. With over 60 participants and 425,000 students assessed, TIMSS 2007 is still the largest study of student math and science achievement in the world. Fourth and eighth grade students were the focus in 2007 and each participating country sampled approximately 4,000 students in 150 schools.

SciMath<sup>MN</sup> sponsored Minnesota's 1995 participation as a 'mini-nation' in TIMSS, and was selected to analyze the 2007 Minnesota TIMSS results, where Minnesota again participated as a mini-nation.

Mini-nation status allows Minnesota to participate as if it were a nation, establishing our ranking among the other participating nations and providing insight into our students' ability to compete on a global scale.

### WHERE WAS MINNESOTA MATHEMATICS IN 2007?

#### MINNESOTA'S 2007 TIMSS MATHEMATICS PERFORMANCE

- ◆ The Minnesota 4<sup>th</sup> grade performance **gain** was among the largest of any of the 16 countries that participated in both the 1995 and 2007 TIMSS ( $p < .05$ ).
- ◆ The Minnesota 4<sup>th</sup> grade **gain**, which was over a third of a standard deviation, was

more than three times the gain indicated for the U.S. as a whole.

- ◆ At 8<sup>th</sup> grade, Minnesota's 2007 **gain** over 1995 was substantially less than the 4<sup>th</sup> grade gain – about one tenth of a standard deviation – which was not statistically significant ( $p < .11$ ).
- ◆ A similar pattern of improvement from 1995 to 2007 for both the U.S. as a whole and Minnesota can be noted with the NAEP results.

### WHERE WAS MINNESOTA SCIENCE IN 2007?

#### 2007 TIMSS SCIENCE PERFORMANCE:

- ◆ In contrast to the performance in mathematics, in science neither the U.S. nor Minnesota demonstrated significantly different performance in 2007 than in 1995.
- ◆ In 2007, Minnesota maintained its relatively high level of performance, being outperformed by very few countries at either 4<sup>th</sup> or 8<sup>th</sup> grade and significantly outperforming the U.S. at grade 8.

**WHAT HAS HAPPENED SINCE  
MINNESOTA PARTICIPATED LAST  
IN 1995?  
MORE THAN A DECADE OF  
ACTION**

Minnesota has not stood idle in the twelve intervening years between these tests. A number of significant statewide educational changes have been implemented:

- State standards in mathematics and science were implemented in 1997 and have since been revised twice.
- Rigorous high stakes tests (Minnesota Comprehensive Assessments) have been in place since 1998 in mathematics (and 2008 for science).
- SciMath<sup>MN</sup> developed Frameworks for teaching mathematics and science (based on Minnesota state standards) that were widely distributed and used throughout Minnesota.
- Standards-based mathematics curriculum increased in use – especially in larger districts, thereby impacting the majority of students in the state.
- Increased classroom time has been allocated in many districts to the tested subjects – especially at the elementary level.
- Graduation requirements in both mathematics and science have significantly increased.
- Algebra will be required for all 8<sup>th</sup> grade students in the year 2011, and Algebra II will be required of the same cohort of students for graduation in 2015; graduates of 2015 must also complete either chemistry or physics. Many districts have already initiated the change process to prepare students for these requirements.
- SciMath<sup>MN</sup> shared Minnesota's participation in the 1995 TIMSS with many districts, which produced valuable lessons for the districts becoming resources for staff development and decision-making.

# MINNESOTA 2007 TIMSS REPORT

## MATHEMATICS - THE REST OF THE STORY

### TEACHING EMPHASIS

Preliminary results for Minnesota on the 2007 TIMSS assessment released in December 2008 and February 2009 indicated that 4<sup>th</sup> grade teachers in Minnesota are distributing their teaching time in closer alignment to teachers in high performing countries, which puts them in closer alignment with the Framework for the TIMSS Assessment. This Framework is also closely aligned with Minnesota's testing expectations as indicated in Test Specifications for the Minnesota Comprehensive Assessment – II. This latter has likely affected teacher practice and adjusted emphasis on strands since 1995 for most teachers.

For example at Grade 4, in 1995 teachers spent about 35% of their time on number, which should be the major focus of instruction at 4<sup>th</sup> grade, based on the TIMSS Framework, practice in high performing countries, and recommendations from multiple organizations and bodies of research. The TIMSS Framework specifies that about 50% of the content at 4<sup>th</sup> grade will be on number. By 2007, teachers reported spending about 55% of their time, on average, on number, much closer to the TIMSS expectations, and no doubt partly influenced by

state testing expectations which specify 40% on number and 15% on patterns and functions, which at 4<sup>th</sup> grade is closely related to number.

Looking at other strands also gives better alignment. In 1995, Minnesota teachers reported spending about 20% of their time on geometry. This increased to 25% in 2007, closer to but still less than the 35% on the TIMSS assessment of the 30% on Minnesota assessments. The 1995 emphasis of only 5% on data increased to about 15% at the 4<sup>th</sup> grade in 2007, matching both the TIMSS distribution and Minnesota test requirements. In 1995 4<sup>th</sup> grade teachers reported spending about 40% of their time on "other", more than any other strand, whereas in 2007 this decreased to less than 5% of their time. This change alone is likely to have affected improved test results. (See Figure 1)

Figure 1b shows how the 2007 MN focus compares to the international focus. Compared to 1995, the variability in the reported percent teacher time devoted to Geometry and Data is greater in 2007. (Figure 1b)

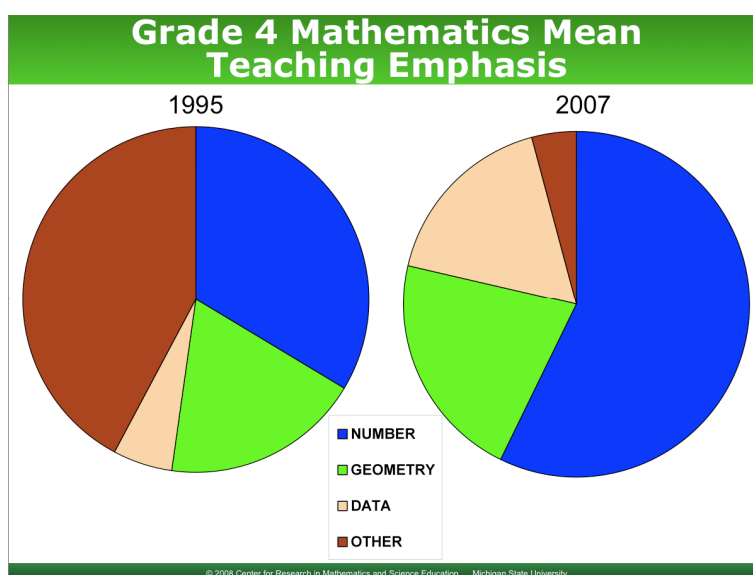
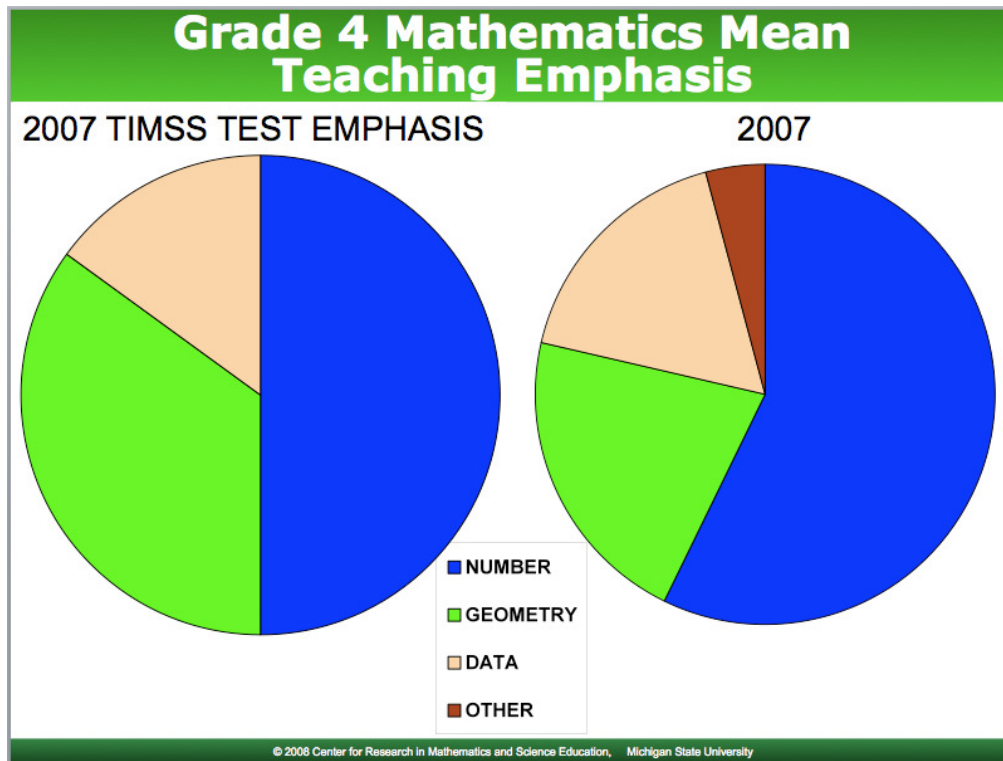
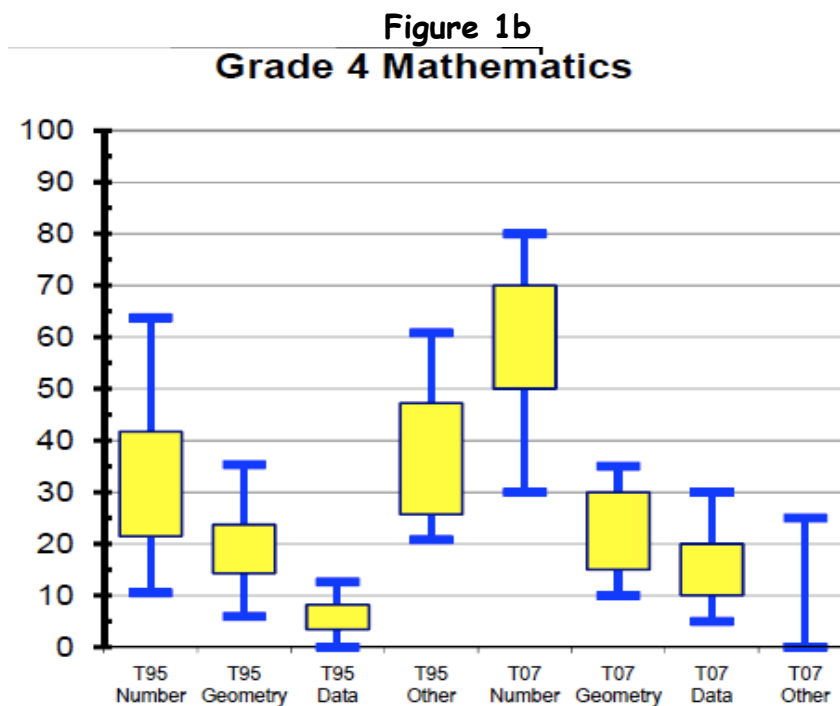


Figure 1



**Figure 1a**  
MINNESOTA TIMSS TEACHING TIME IN 1995 AND 2007



At the 8<sup>th</sup> Grade there is a similar story with regard to all strands, especially algebra, which is a major focus of instruction at this grade in the top performing countries, the TIMSS Content Framework, and Minnesota's 2007 standards (which were not in place at the time of the 2007 TIMSS assessment).

In 1995 8<sup>th</sup> grade Minnesota teachers reported spending about 10% of their time on algebra; this changed to nearly 50% in 2007. TIMSS Specifies 30%; Minnesota also specifies 30%. For the Number strand, in 1995 8<sup>th</sup> grade teachers reported spending about 40% on number; by 2007 this was reduced to 20%. TIMSS indicates 30% for Number at grade 8, while Minnesota specifies about 25%.

There was little change for the Geometry strand, with teachers reporting about

15% for both 1995 and 2007. TIMSS indicates 20% for Geometry at grade 8, while Minnesota specifies 30%.

For the Data strand, teachers moved from about 5% in 1995 to 15% in 2007, matching the Minnesota test specifications of 15%, but slightly less than the TIMSS Framework indicator of 20%.

Finally, as at 4<sup>th</sup> grade, the category of "Other", which represented about 30% of time in 1995, was less than 5% in 2007. (See Figure 2) Figure 2b shows how the 2007 math focus compared to the international focus. Compared to 1995, the variability in the reported percent of teacher time devoted to Geometry and Algebra is greater in 2007. (Figure 2b)

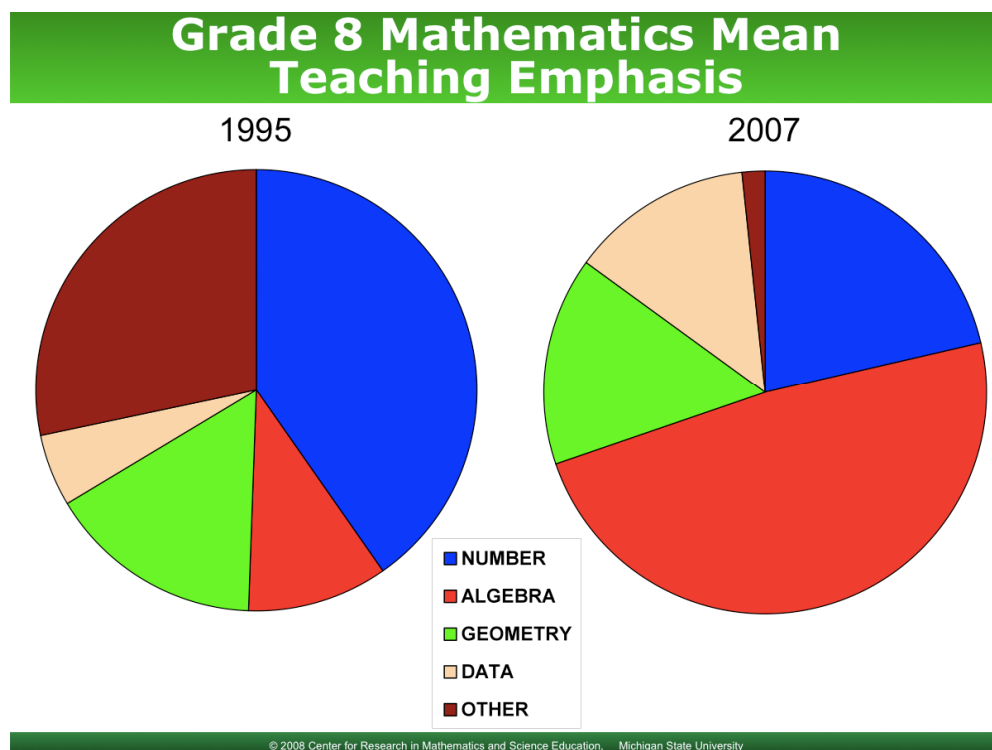


Figure 2

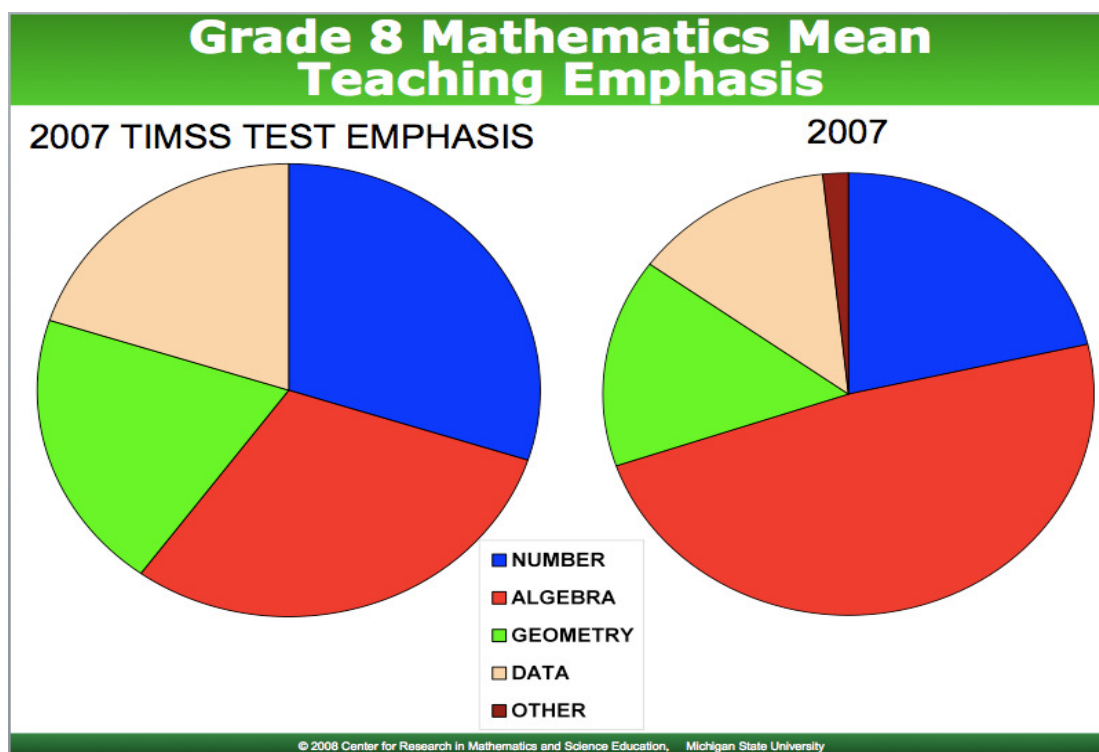


Figure 2a

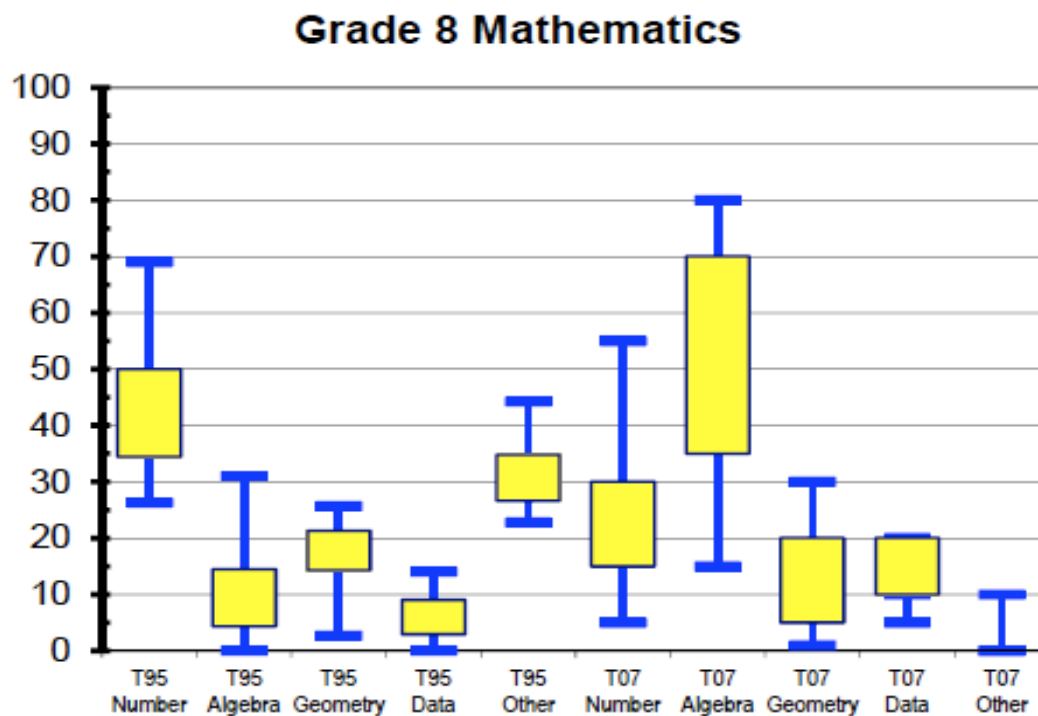


Figure 2b

- A major shift in the implemented curriculum is apparent in 8th grade. This is evident from the increase in reported percent teaching time devoted to Algebra. On average (Median), in 2007 MN teachers report spending more than 50% of teaching time on Algebra topics compared to less than 10% of teaching time on the same topics in 1995.
- The percentage of reported time on coverage of Data Representation also shows an increase-median percentage of approximately 15% in 2007 compared to approximately 5% in 1995.
- The reported percent time on Number, Geometry and “other” mathematics topics show a decrease in 2007 compared to 1995.

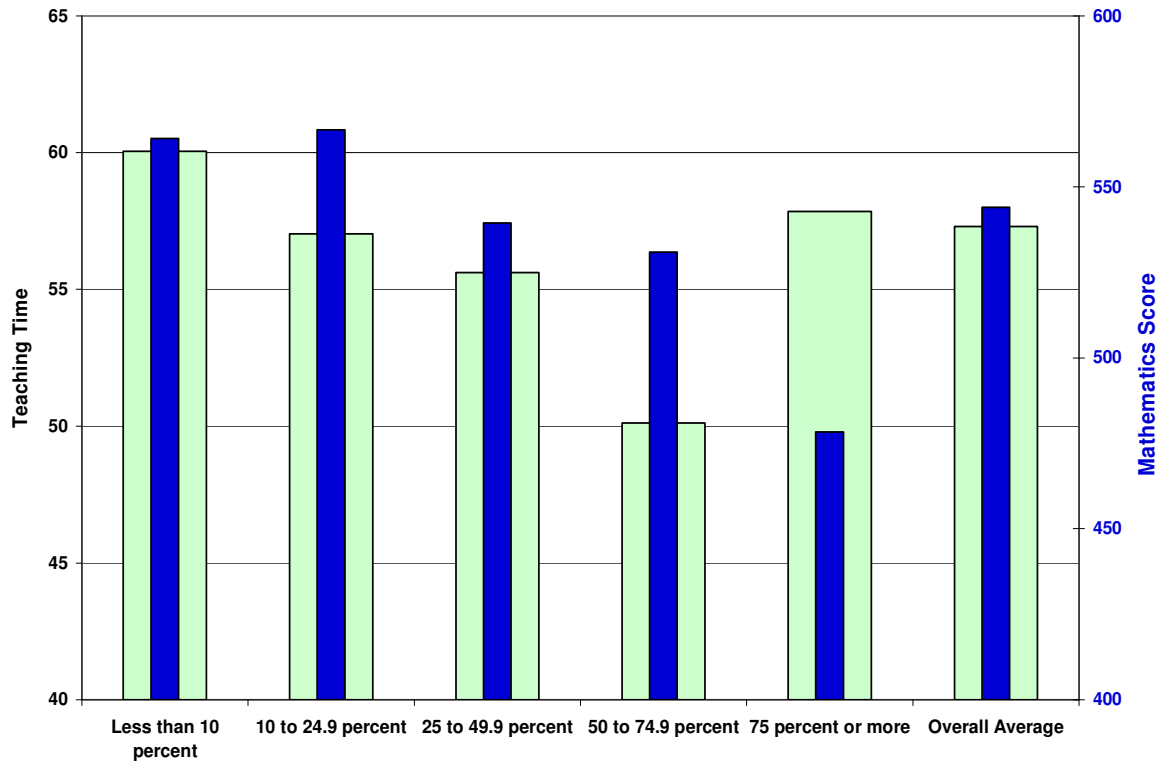
### **Race/ minority status**

There is some data on the performance of students in schools with different proportions of minority enrollment.

For 4<sup>th</sup> grade students, on the number strand, those in schools with 25% or less of minority enrollment performed the highest, on par with Japan, and above the overall Minnesota average. Students in schools with minority enrollment between 25 and 75% minority performed less well, slightly below the US average. Students in schools with more than 75% minority students performed least well, placing them between the Ukraine and Iran.

Teachers in schools with more than 75% minority enrollment spend about the same proportion of their teaching time on number as most teachers in Minnesota; nevertheless their students perform less well. (Figure 3)

## Grade 4 Teaching Time in Number and Mean Mathematics Score by Percentage of Minority Student Enrollment in School



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Figure 3

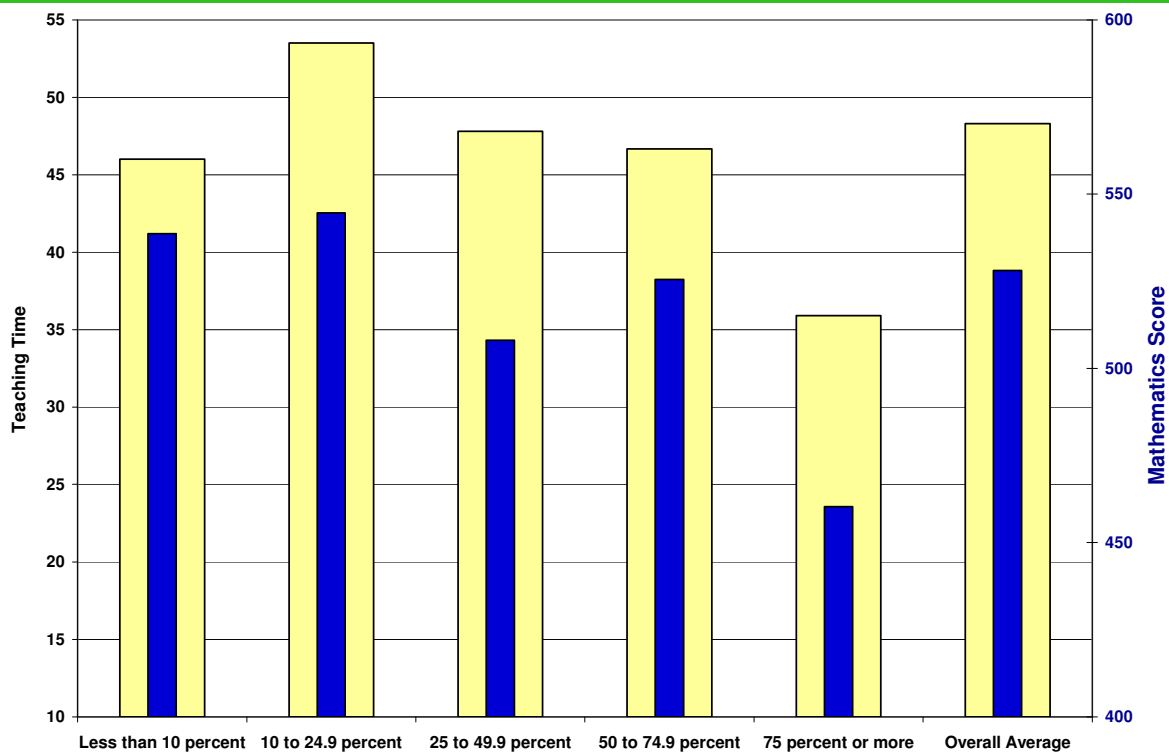
At the 8<sup>th</sup> grade, a similar result occurs on the algebra strand. Students in schools with less than 25% minority enrollment score better than the Minnesota average, those in schools with between 25 and 75% minority enrollment score at approximately the Minnesota average, and those in schools with more than 75% minority enrollment are considerably below the others, again at about

the achievement level of the Ukraine, though above Iran.

8<sup>th</sup> grade teachers in schools with more than 75% minority enrollment report spending about 35% of their time on algebra, less than the 47% of the average 8<sup>th</sup> grade Minnesota teacher. (Figure 4)



## Grade 8 Teaching Time in Algebra and Mean Mathematics Score by Percentage of Minority Student Enrollment in School



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Figure 4

### SOCIO-ECONOMIC STATUS

When students are disaggregated by Socio-Economic Status (SES), qualification for Free or Reduced price Lunch (FRL) is used as a marker, since qualification is based on poverty guidelines.

Looking at 4<sup>th</sup> grade student overall scores, Minnesota students in schools where less than 25% of the students qualify for FRL perform the highest, above the overall average. Students in schools with between 25

and 50% FRL perform at about the Minnesota average, while students in schools with between 50 and 75% FRL perform below the state average.

Schools where more than 75% of students qualify for FRL perform well below the Minnesota average. In all cases, Minnesota students perform above the US average for the group. (Figure 5)

## Grade 4 Mathematics Means in MN and the USA by Percentage of Students in School Eligible for Free or Reduced Lunch

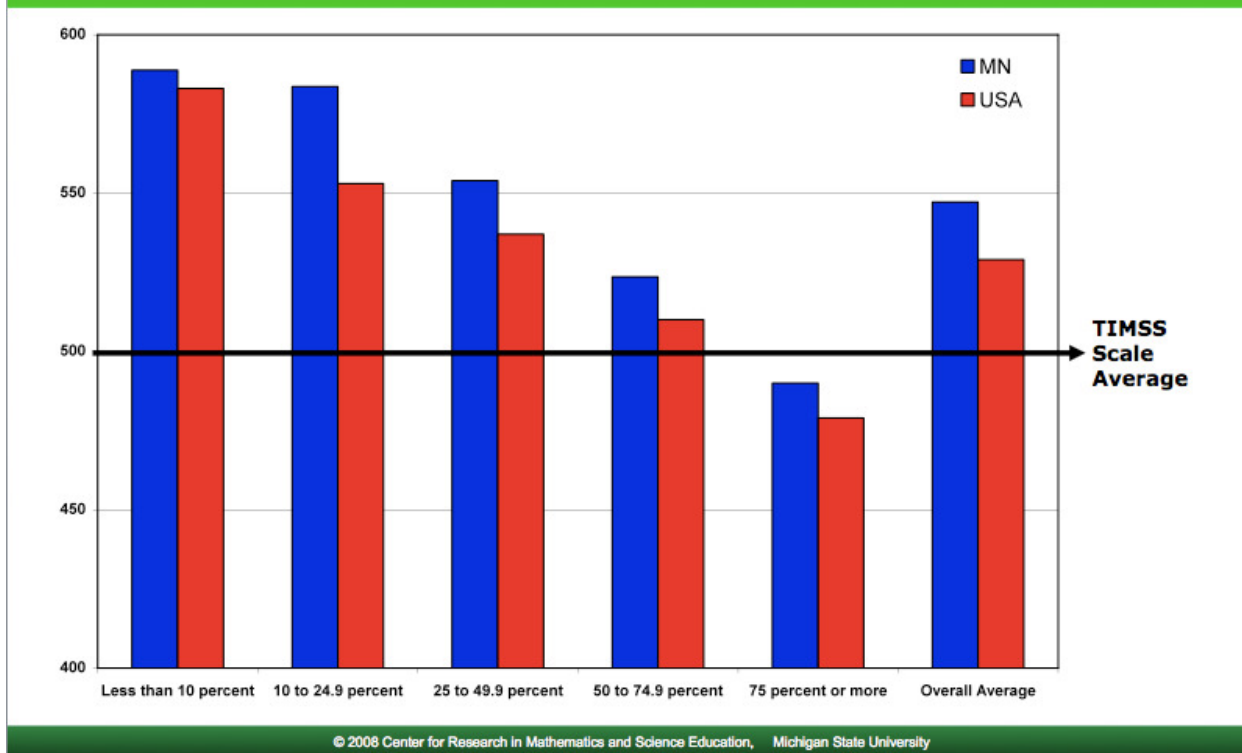


Figure 5

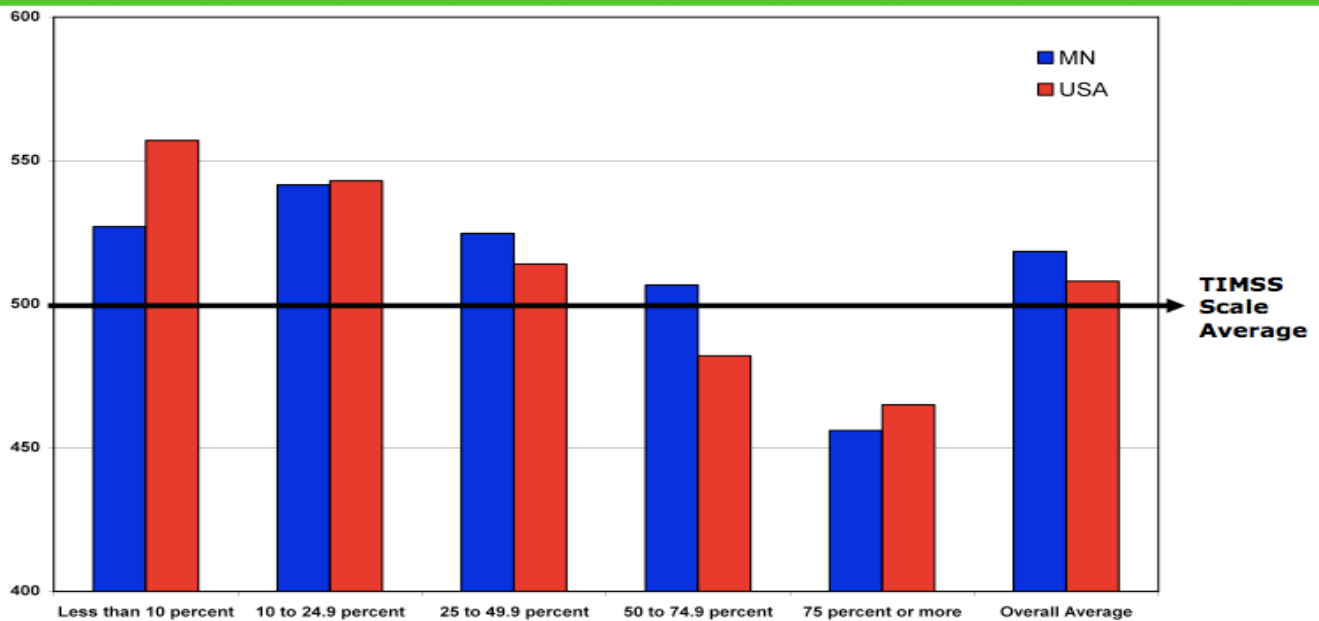
At the 8<sup>th</sup> grade, the pattern is somewhat different. Students in schools with less than 10% FRL perform just slightly above the Minnesota average, and below the US average. For those in schools with 10-25% FRL, Minnesota students perform above their peers in more affluent schools, above the Minnesota average, and nearly as well as the US average.

Students in schools with between 25 and 75% FRL perform at approximately the Minnesota average and above the US average. Students in high poverty schools, those with more than 75% FRL, perform well below the Minnesota average, and below the US average for students in similar schools. (Figure 6)

For 4<sup>th</sup> grade, a similar pattern is evidenced when looking at the number strand. There is a steady decrease in performance on TIMSS as the proportion of students eligible for FRL increases. (Figure 7)

At the 8<sup>th</sup> grade, the results for the algebra strand exhibit a different pattern. The Minnesota average is about 525, and students in schools with less than 75% FRL all hover around that score, ranging from about 515 to about 540. However, students in schools with more than 75% FRL average about 450 in algebra, putting them far behind their peers. Their teachers also report spending less time on algebra than their counterparts in other schools. (Figure 8)

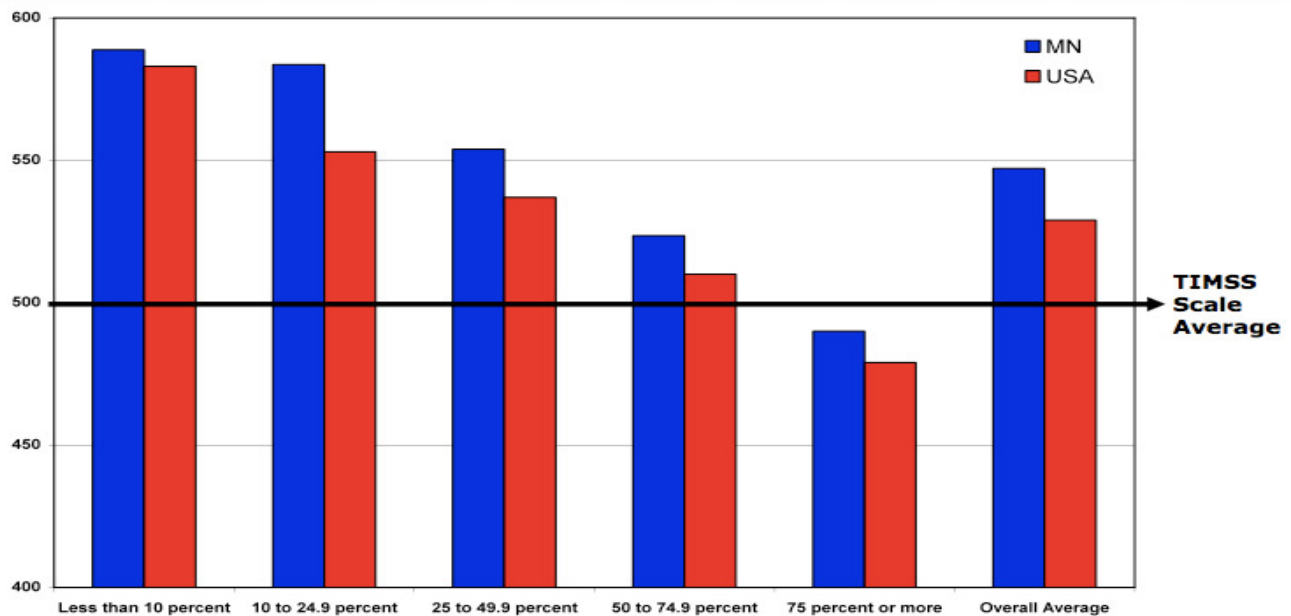
## Grade 8 Mathematics Means in MN and the USA by Percentage of Students in School Eligible for Free or Reduced Lunch



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Figure 6

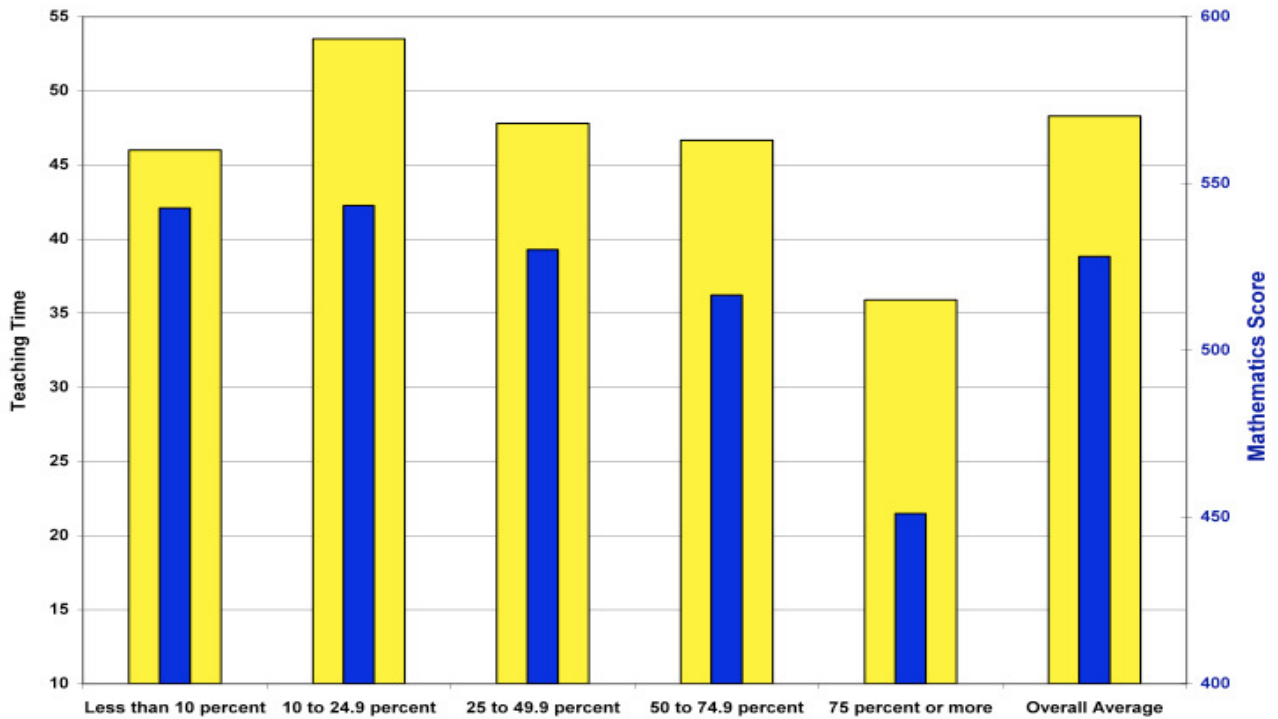
## Grade 4 Mathematics Means in MN and the USA by Percentage of Students in School Eligible for Free or Reduced Lunch



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Figure 7

## Grade 8 Teaching Time in Algebra and Mean Mathematics Score by Percentage of Students in School Eligible for Free or Reduced Lunch



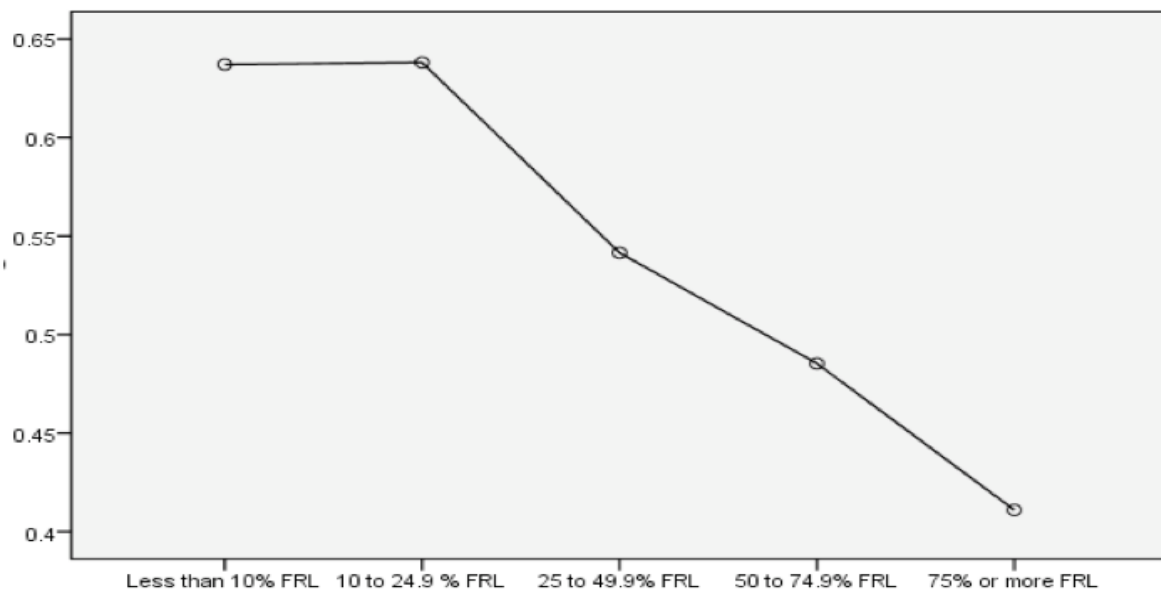
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Figure 8

Looking at substrand data for 4<sup>th</sup> grade over SES gives a picture similar to other data for 4<sup>th</sup> grade. There is a decline in performance as the percent of students eligible for FRL increases. For Whole Number Operations,

scores range from about 63% correct for students in schools with less than 25% FRL to about 40% for schools with more than 75% FRL. (Figure 9).

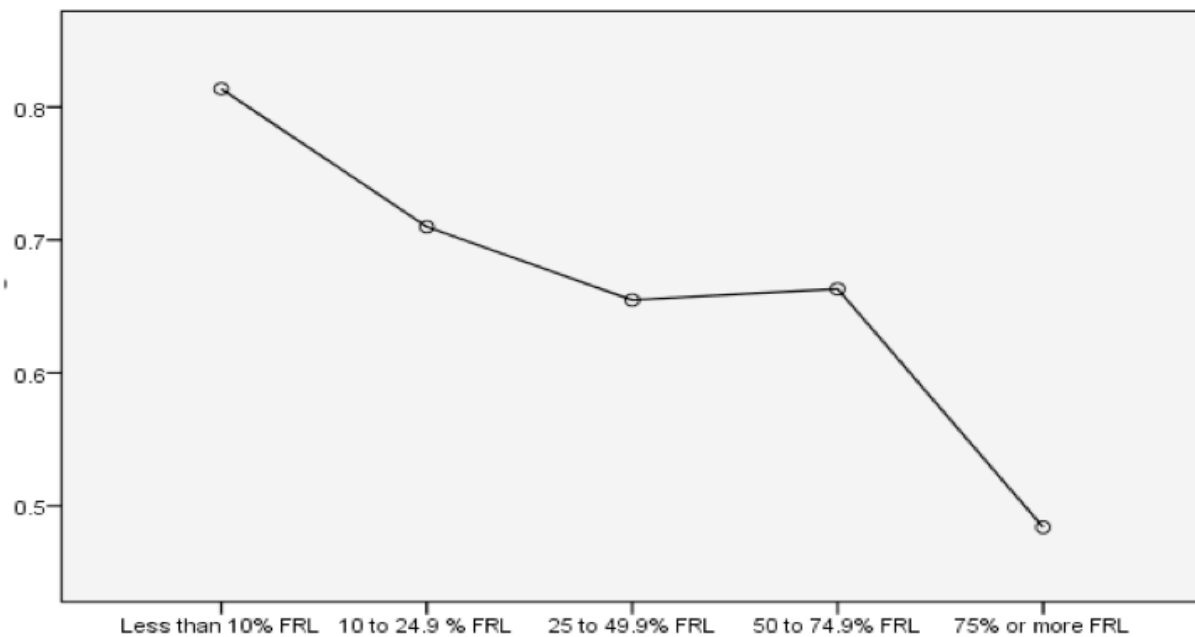
### Grade 4 Whole Number Operation: Average Percent Correct by SES



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Figure 9

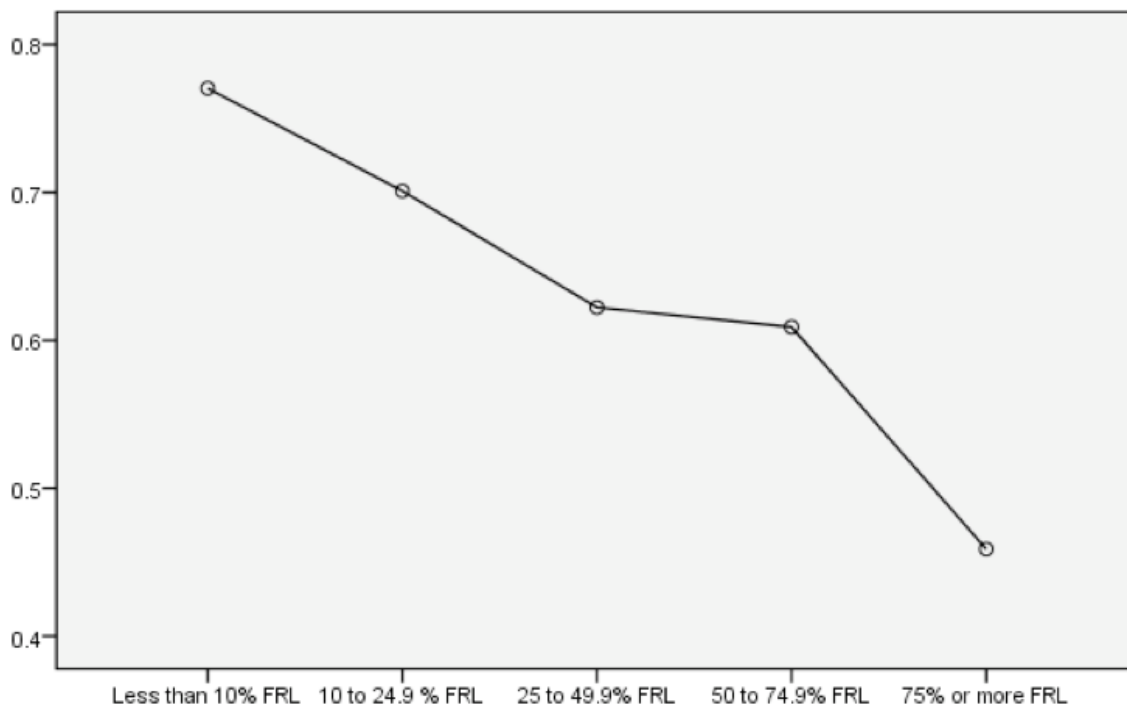
### Grade 4 Common Fractions: Average Percent Correct by SES



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Figure 10

## Grade 4 Decimal Fractions: Average Percent Correct by SES



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Figure 11

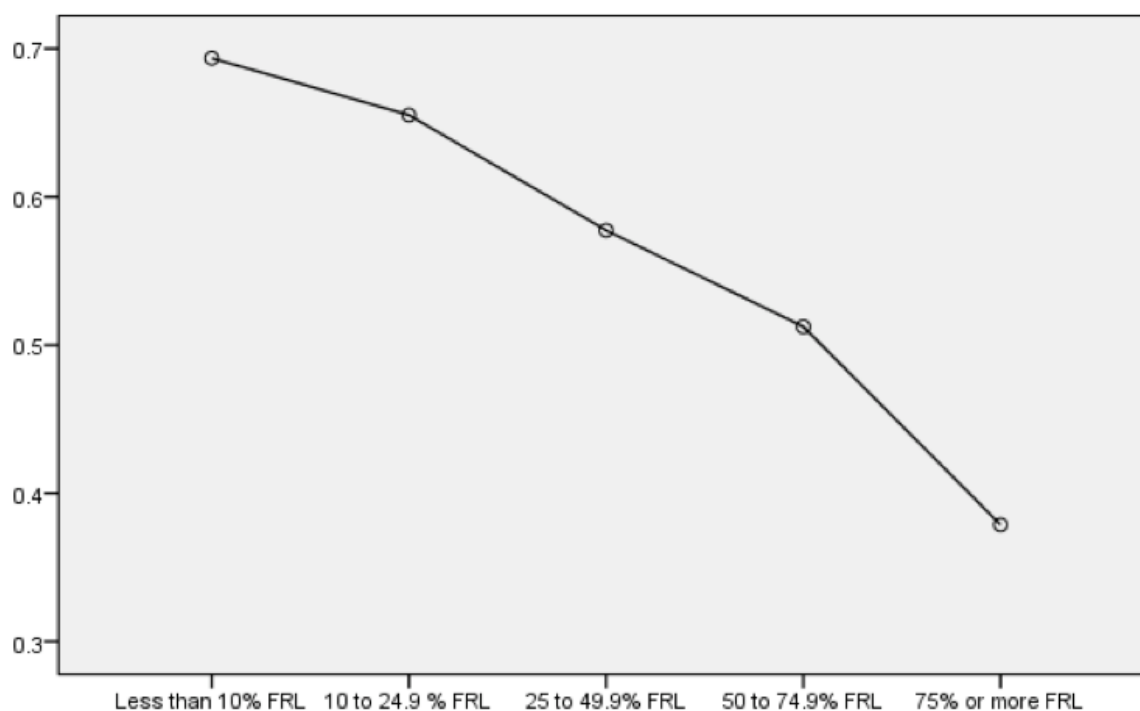
For the Common Fraction substrand at grade 4, students in schools with less than 10% FRL answered more than 80% of the items correctly, while students in schools with more than 75% FRL answered less than 50% correctly. (Figure 10)

On Decimal Fractions, correct responses ranged from almost 80% correct for students in schools with less than 10% FRL to less than

50% for schools with more than 75% FRL. (Figure 11)

On the Measurement Units substrand at grade 4, there is a similar decrease, with students in schools with less than 10% FRL answering about 70% of items correctly, while students in schools with more than 75% FRL answer less than 40% correctly. (Figure 12)

## Grade 4 Measurement Units: Average Percent Correct by SES



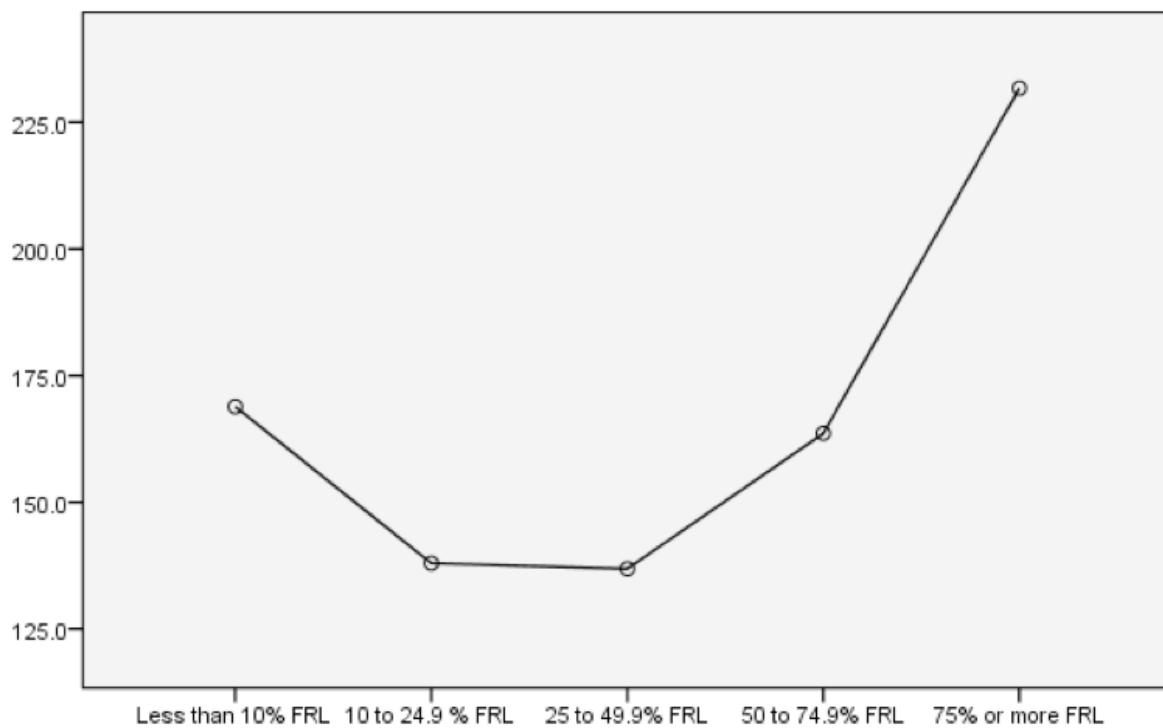
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Figure 12

When we consider total instructional time at grade 4, the picture that emerges is somewhat different. Teachers in schools with more than 75% FRL spend the largest amount of time on mathematics, a total of about 225 hours per year, or 75-90 minutes per day.

On the other hand, teachers in schools with less than 10% FRL, and those in schools with between 50 and 75% FRL spend slightly more than one hour per day on mathematics. Teachers in schools with between 10 and 50% FRL report spending about 45 minutes per day on mathematics instruction. (Figure 13)

## Grade 4 Yearly Total Mathematics Instructional Time by SES



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Figure 13



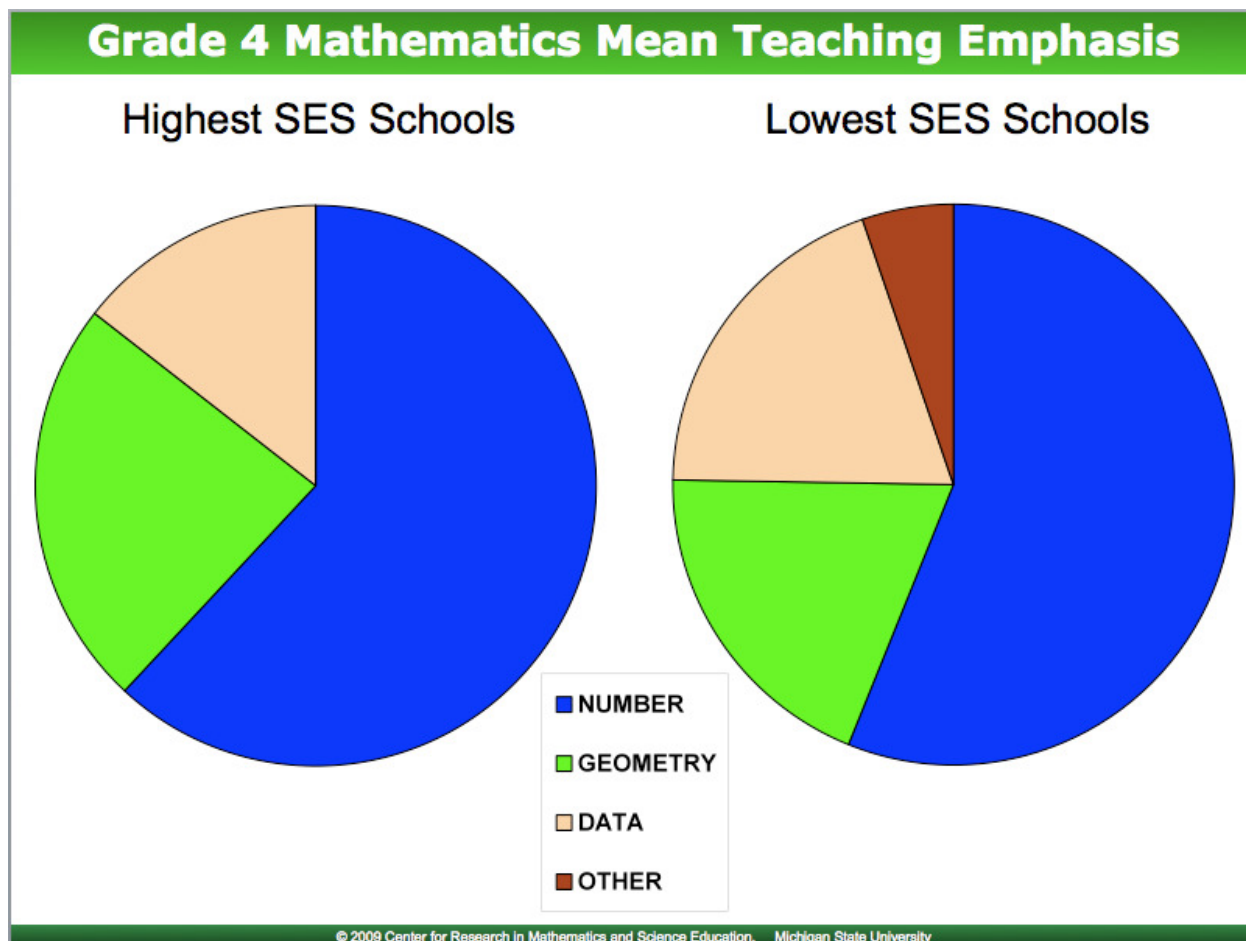


Figure 14

At 4<sup>th</sup> grade there are also differences in teacher emphasis across SES. Teachers in the highest SES schools spend more time on number and geometry than teachers in the lowest SES schools. Teachers in the highest SES schools spend no time on the “other” category; teachers in the lowest SES schools spend about 5% of their time on “other”. (Figure 14)

The variation between them is the difference between 62% for the highest SES schools on number, and 56% for the lowest. This amounts to a difference of more than 2 weeks of instruction. For geometry, the differences are about 5%, so the high SES schools have about 2 weeks more of geometry instruction. The amount of time the low SES schools spend on “other” also translates into about 2 weeks. (Figure 15)

## Mean Percent of Grade 4 Mathematics Teaching Time

| <i>Topic</i> | <i>Highest SES</i> | <i>Lowest SES</i> | <i>Difference</i>   |
|--------------|--------------------|-------------------|---------------------|
| Number       | 62                 | 56                | <b>&gt; 2 Weeks</b> |
| Geometry     | 24                 | 19                | <b>~ 2 Weeks</b>    |
| Other        | 0                  | 5                 | <b>~ 2 Weeks</b>    |

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Figure 15

At the 8<sup>th</sup> grade level, the data on substrands gives a picture similar to that at 4<sup>th</sup> grade, but is often more dramatic. For example, on the Common Fractions substrand, there is a 5% decline between the scores of students in schools with less than 10% FRL and schools in the 50 to 75% FRL range. However, the drop from scores of students in the 50 to 75% FRL is about 20%. (Figure 16)

For Congruence and Similarity, the decline from 1 to 75% is 4%, while the drop from 50 to 75% to more than 75% FRL is about 12%. (Figure 17)

For Proportion Concepts, there is a 2% drop from the schools with less than 10% FRL to those between 50 and 75%, but from the

latter to students in schools with more than 75% FRL there is a 20% drop. (Figure 18)

For Proportion Problems, there is a 16% drop from the schools with less than 10% FRL to those between 50 and 75%, but from the latter to students in schools with more than 75% FRL there is a 22% drop. (Figure 19)

For Functions, the drop from schools with less than 10% FRL to those with between 50 and 75% FRL is about 7 points, while the drop from there to students in schools with more than 75% FRL is about 19%. (Figure 20)

And for Equations, the corresponding numbers are 6% and 20%. (Figure 21)

In other words, students in schools with less than 75% FRL do not perform much differently from each other, though there is slight drop in achievement for students as the

percentage of poor students increases. However, students in schools with more than 75% FRL perform substantially below those in schools with less than 75% FRL.

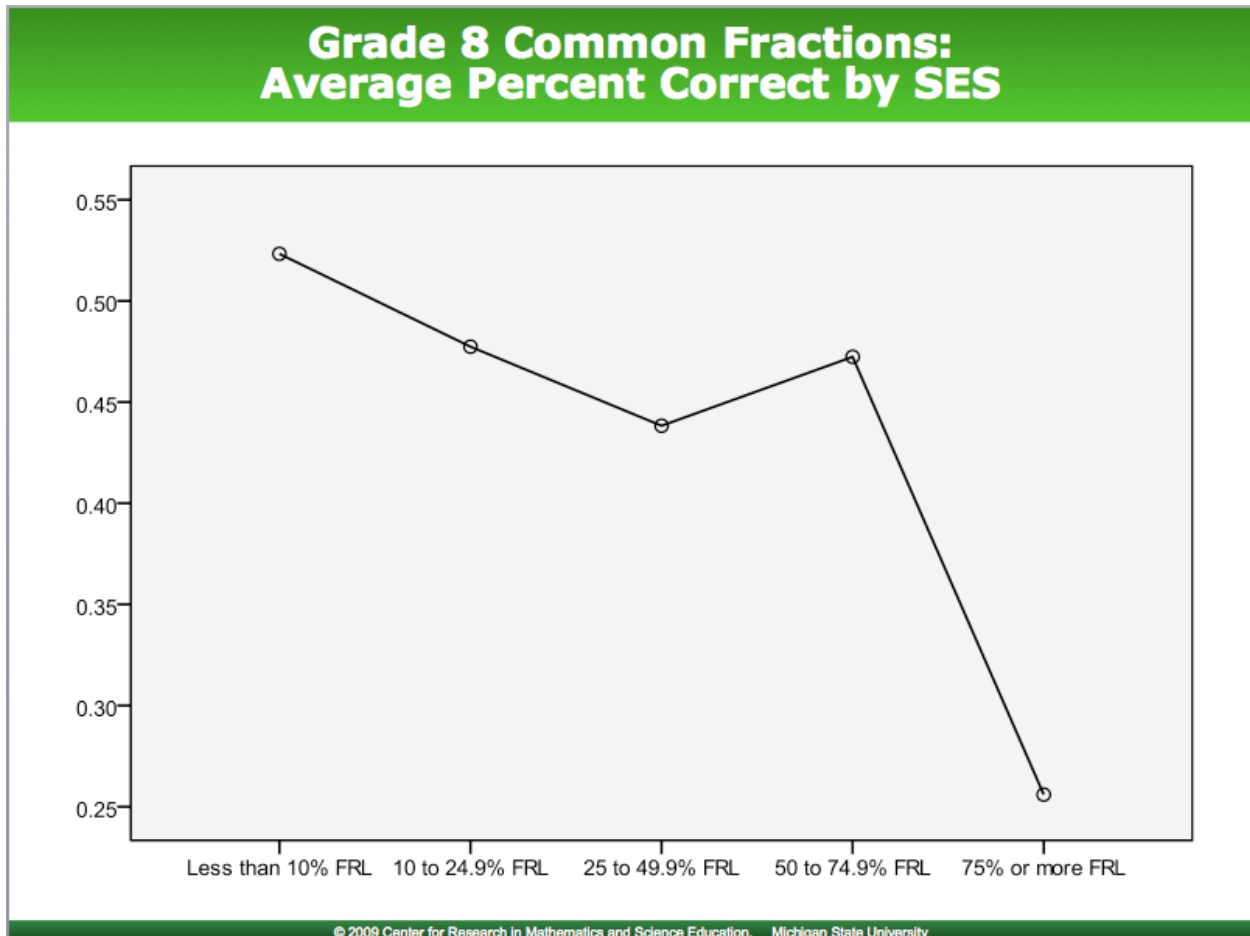
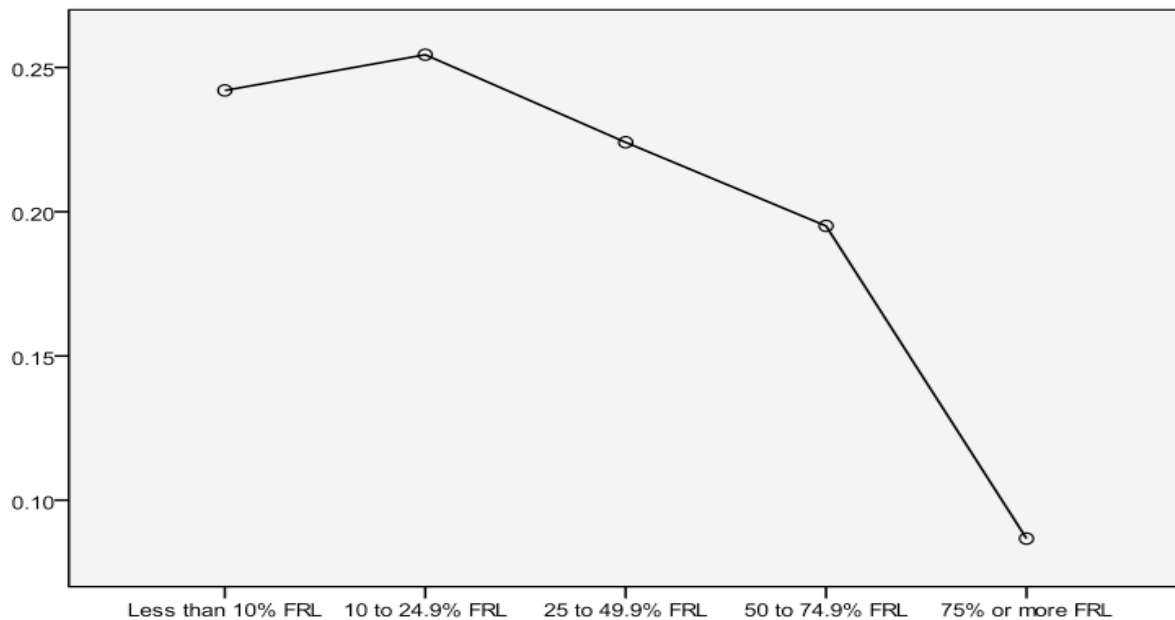


Figure 16

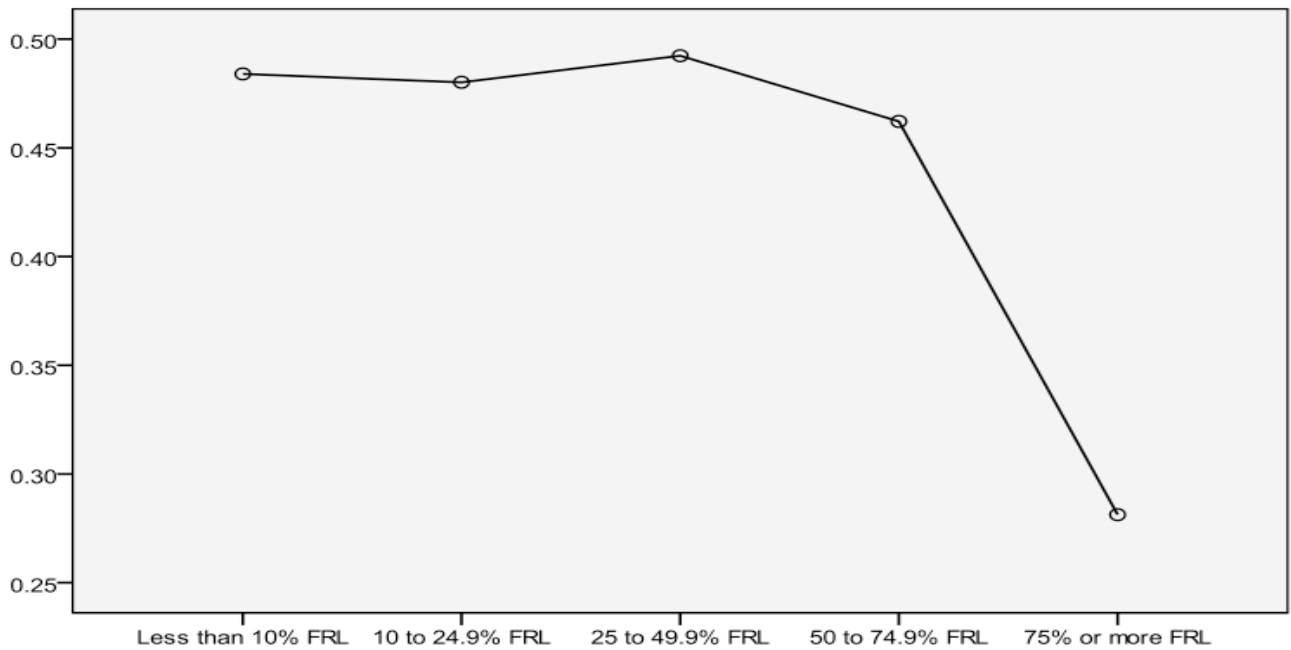
### Grade 8 Congruence and Similarity: Average Percent Correct by SES



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Figure 17

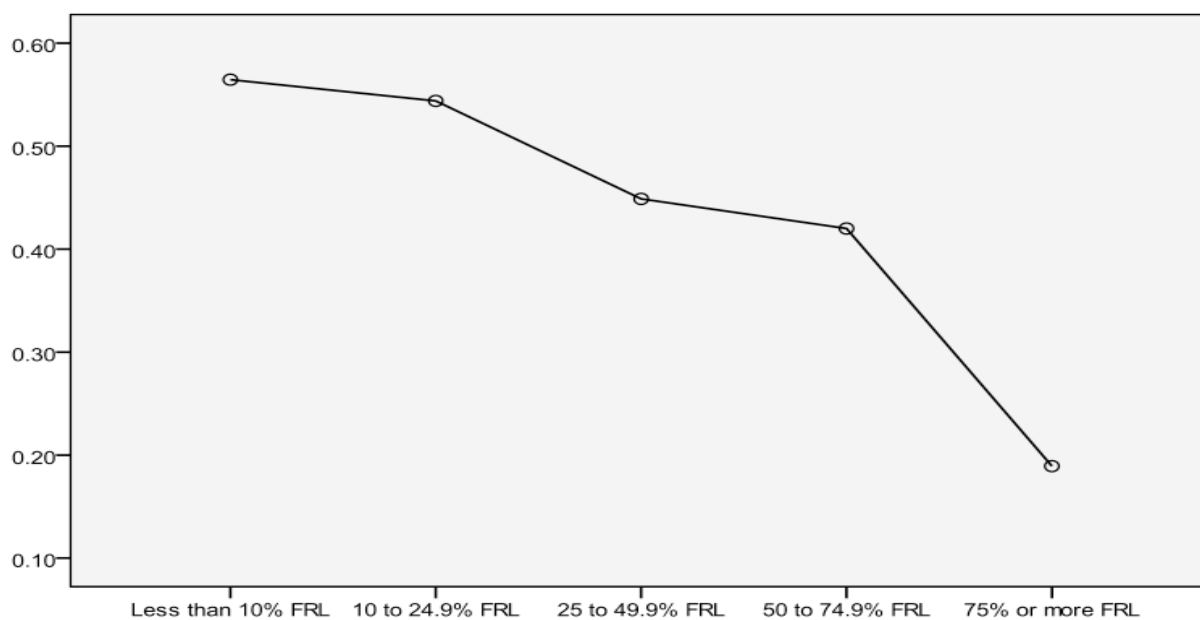
### Grade 8 Proportionality Concepts: Average Percent Correct by SES



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Figure 18

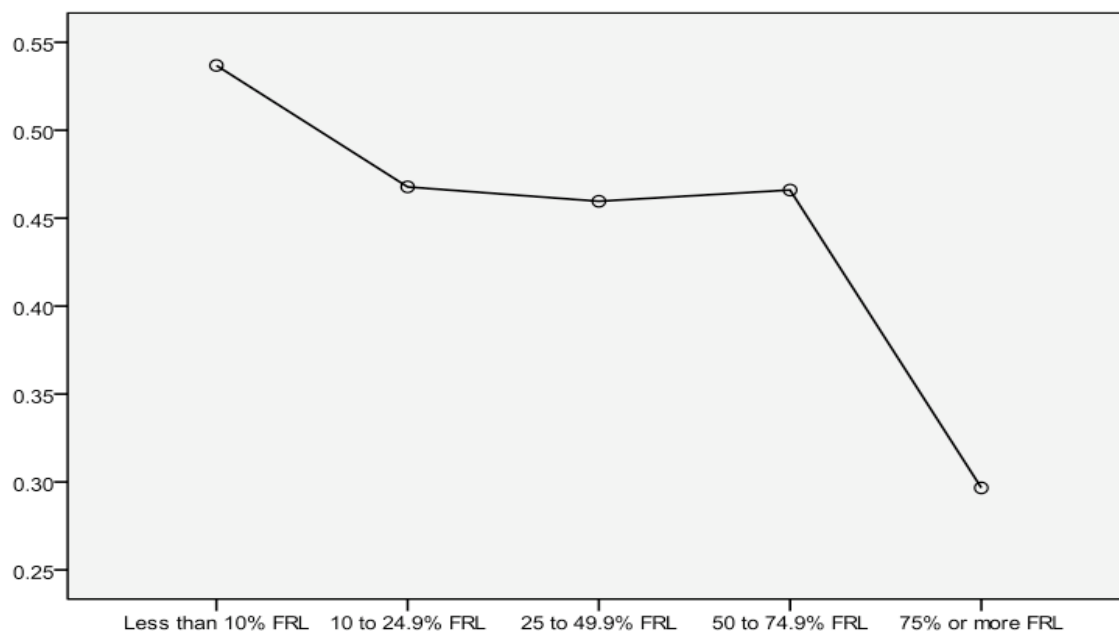
### Grade 8 Proportionality Problems: Average Percent Correct by SES



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Figure 19

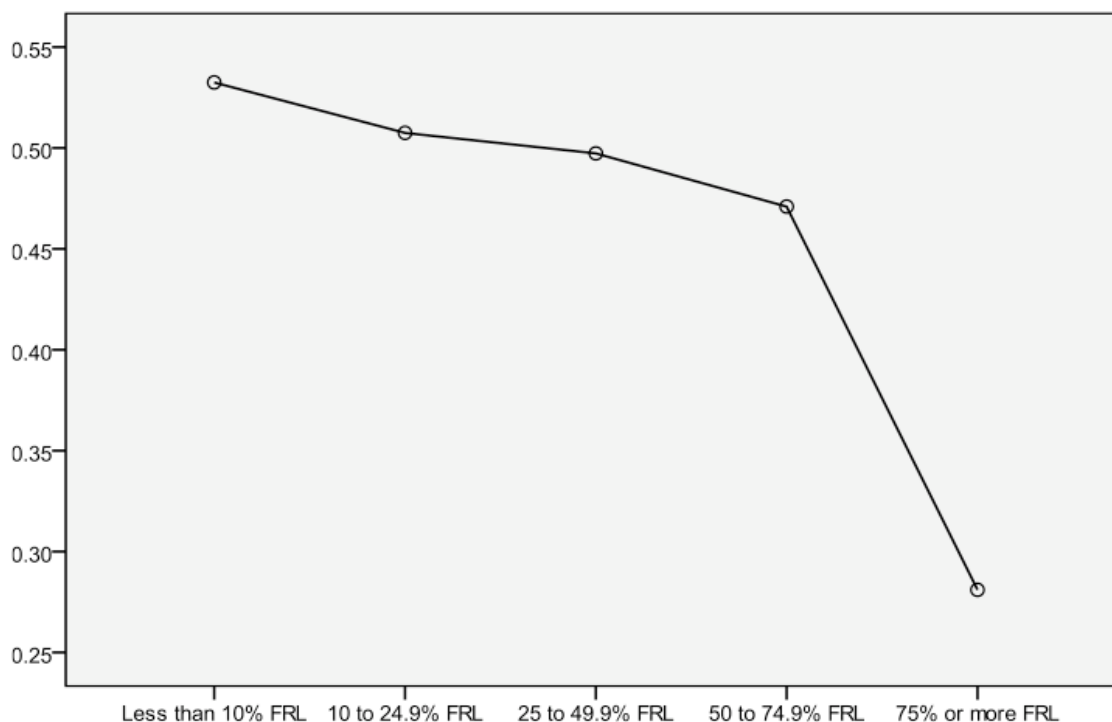
### Grade 8 Functions: Average Percent Correct by SES



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Figure 20

## Grade 8 Equations: Average Percent Correct by SES



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Figure 21

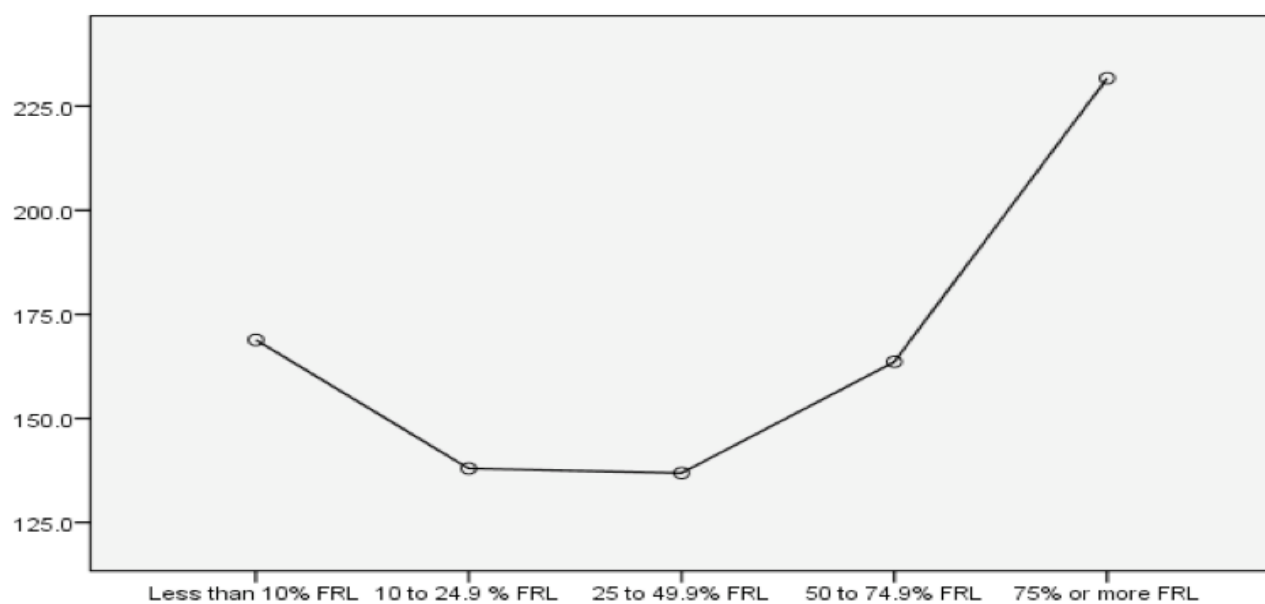
Looking at total time in mathematics across SES groups at grade 8, we see a direct relationship between the percent of students in poverty and time spent on mathematics. That is, the lower the proportion of low SES students in a school, the less time they spend on mathematics.

Students in schools with less than 10% FRL spend about 50 minutes per day in mathematics, the least amount of time for any group. Students in other schools vary

between an average of 50 and 60 minutes, with the most time occurring at schools with between 50 and 75% FRL. (Figure 22)

There are also discrepancies in teacher emphasis at Grade 8. Looking at the key strands of Algebra, Geometry and Number, we find that students in the highest SES schools spend about 4 weeks more per year in Algebra, 2 weeks more on Geometry, and 6 weeks less on Number. (Figure 23, 24)

## Grade 4 Yearly Total Mathematics Instructional Time by SES



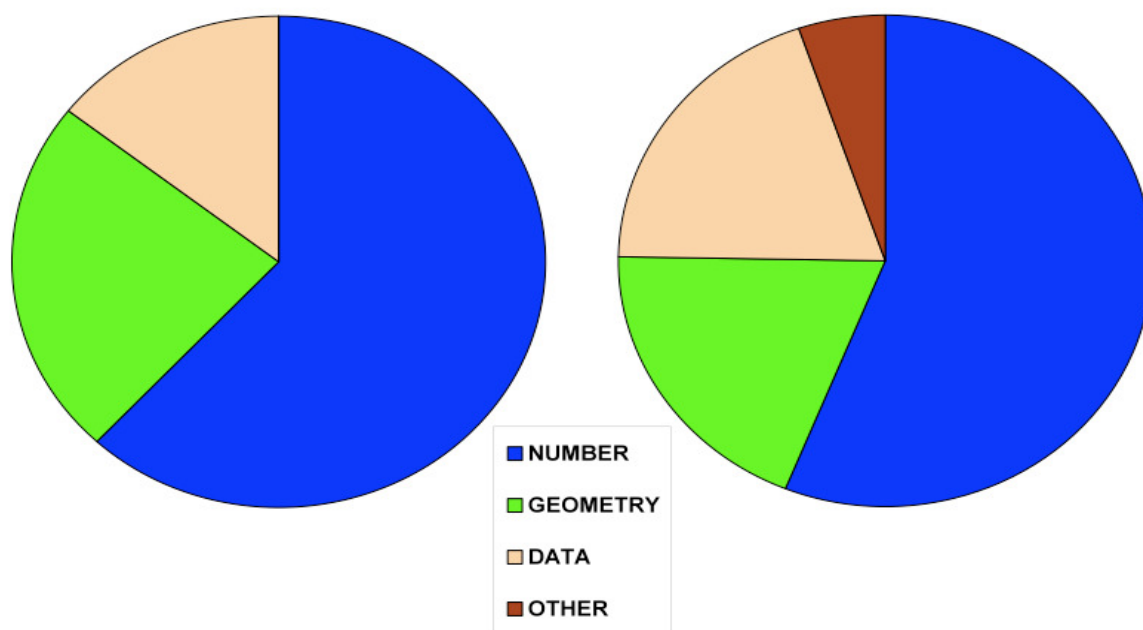
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Figure 22

## Grade 4 Mathematics Mean Teaching Emphasis

Highest SES Schools

Lowest SES Schools



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Figure 23

## Mean Percent of Grade 4 Mathematics Teaching Time

| <i>Topic</i> | <i>Highest SES</i> | <i>Lowest SES</i> | <i>Difference</i>   |
|--------------|--------------------|-------------------|---------------------|
| Number       | 62                 | 56                | <b>&gt; 2 Weeks</b> |
| Geometry     | 24                 | 19                | <b>~ 2 Weeks</b>    |
| Other        | 0                  | 5                 | <b>~ 2 Weeks</b>    |

Figure 24

### NATIONAL ASSESSMENT OF EDUCATIONAL PROGRESS (NAEP) AND TIMSS

Minnesota students continue to perform well on NAEP compared to students in most other states, scoring in the top tier of states for both 4<sup>th</sup> and 8<sup>th</sup> grades. For the 2009 NAEP administration for mathematics, at grade 4, about 42% of Minnesota students are proficient, and about 11% are advanced.

At grade 8, about 37% are proficient while about 13% are advanced. On NAEP, as on TIMSS 2007, Massachusetts's students outperform Minnesota students at both grades 4 and 8. (Figures 25, 26)



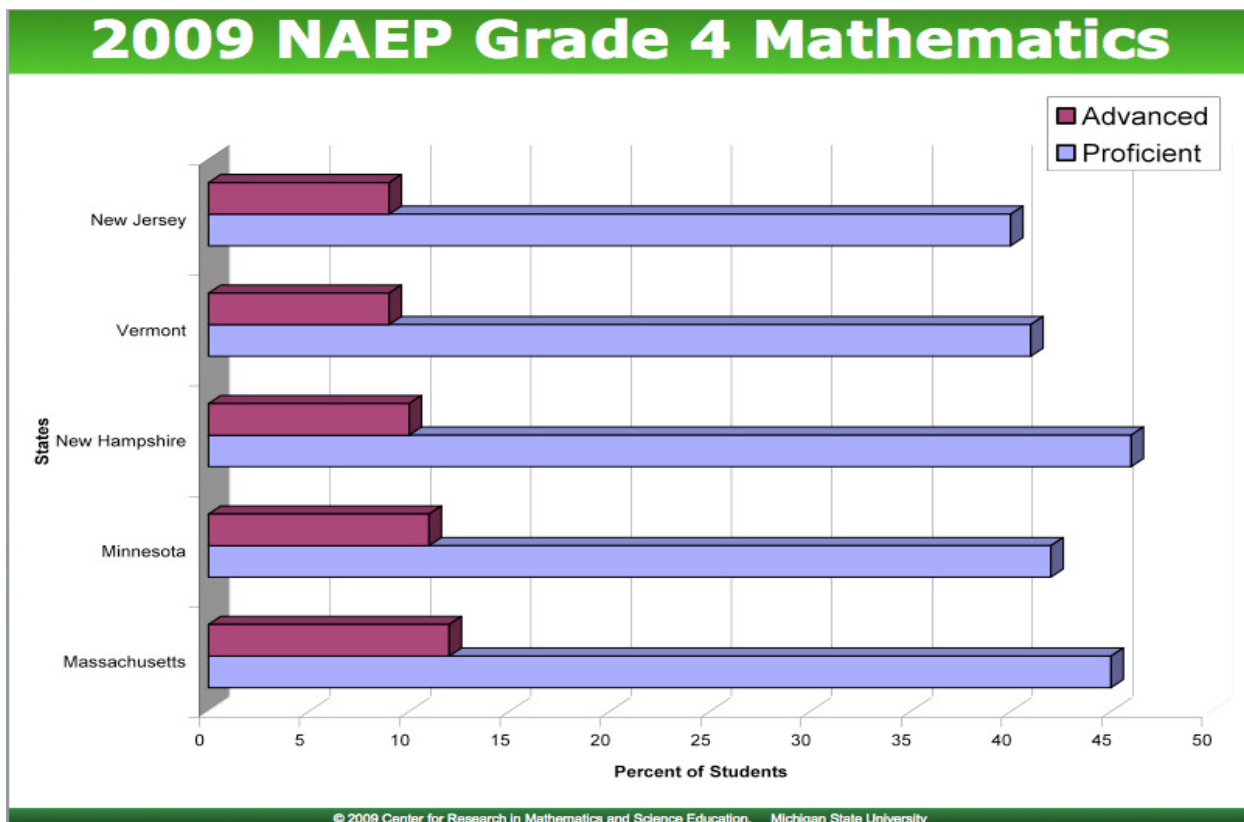


Figure 25

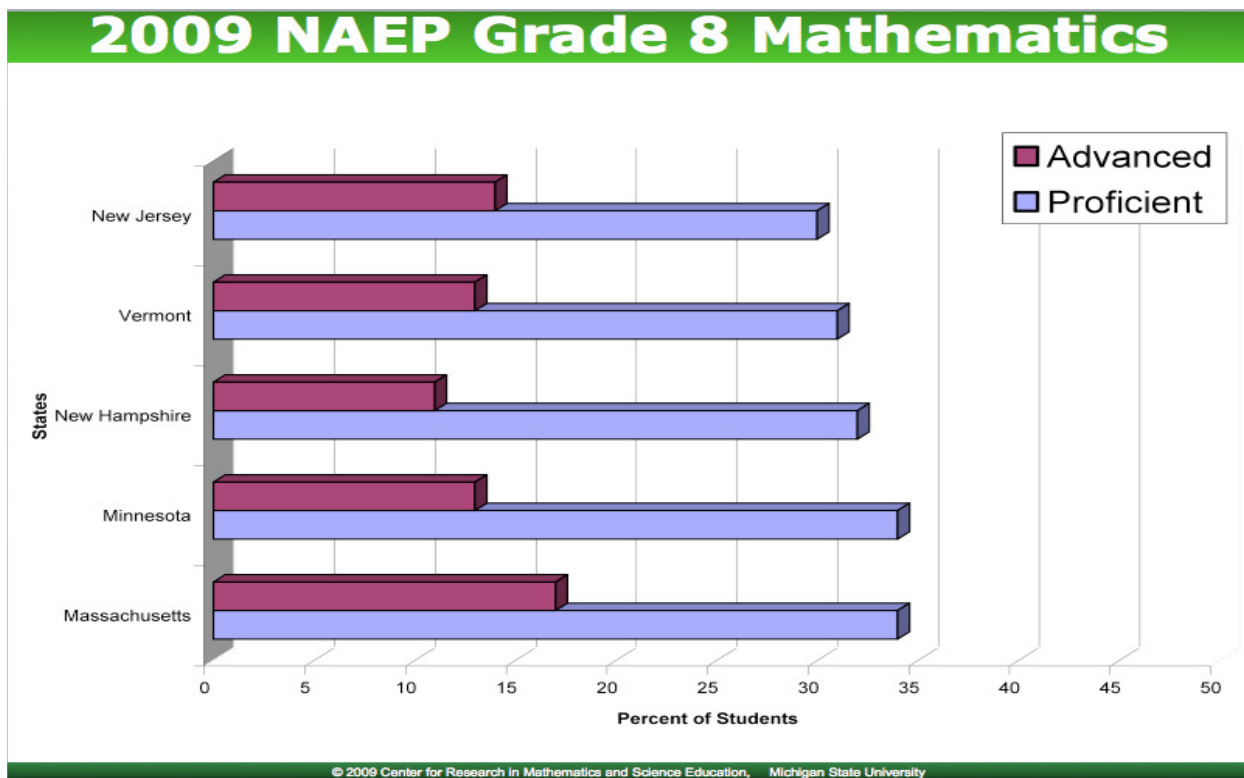


Figure 26

## CONTENT - SUB STRANDS

TIMSS test items were coded into broad categories of mathematics topics. For 4th grade there were 14 categories for mathematics and for 8th grade there were 21 categories the same categories were used in the 1995 analysis.

Student performance for Minnesota and the other countries/benchmarking participants was calculated for each of the categories and statistical tests were conducted to determine Minnesota students' performance relative to the students in other participating countries. The countries included in the comparisons are ones that participated in both 1995 and 2007.

Displays were constructed for categories that contained four or more items. Student performance is represented in terms of percentage of items correct in each category. At grade 4, Minnesota students only scored significantly lower than students in three countries-Hong Kong, Singapore and Japan. Minnesota students scored significantly lower than students in:

- Hong Kong on all twelve broad mathematics categories displayed.
- Singapore on ten broad mathematics categories.
- Japan on four broad mathematics categories

Minnesota students scored significantly higher than the US students in six broad categories of mathematics-Common and Decimal Fractions; Measurement Units; Perimeter, Area and Volume; Geometry: Positions and Shapes; and Symmetry, Congruence and Similarity. Although

Minnesota students scored higher than the US students in the other six broad categories, the differences were not statistically significant. (Figure 27 - Display 1)

At grade 8 Minnesota students scored significantly lower than students in seven countries or benchmark participants-Hong Kong, Singapore, Rep. of Korea, Japan, England, the Russian Federation and Quebec. Minnesota students scored significantly lower than students in:

- Rep. of Korea on fifteen broad mathematics categories.
- Singapore on fourteen broad mathematics categories.
- Hong Kong on twelve broad mathematics categories.
- Japan on nine broad mathematics categories.

Minnesota students scored significantly higher than the US students in eight broad categories of mathematics-Decimal Fractions and Percents, Relations of Fractions, 2-D and 3-D Geometry, Perimeter, Area and Volume, Data Representation and Uncertainty-Probability.

Although Minnesota students scored higher than the US students in all other broad categories, the differences were not statistically significant. (Figure 28 - Display 3, two parts)

Display 1: Grade 4 Mathematics Topics

| Meaning of Whole Numbers | Whole Number Operations  | Common Fractions         | Decimal Fractions        | Measurement Units        | Perimeter, Area & Volume |
|--------------------------|--------------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| HONG KONG SAR 80         | HONG KONG SAR 75         | SINGAPORE 76             | SINGAPORE 83             | HONG KONG SAR 74         | HONG KONG SAR 78         |
| JAPAN 77                 | SINGAPORE 74             | HONG KONG SAR 75         | HONG KONG SAR 73         | SINGAPORE 69             | SINGAPORE 73             |
| SINGAPORE 74             | JAPAN 60                 | MINNESOTA, US 68         | MINNESOTA, US 65         | JAPAN 68                 | JAPAN 65                 |
| NETHERLANDS 71           | LATVIA 60                | ENGLAND 62               | ENGLAND 57               | NETHERLANDS 67           | MINNESOTA, US 63         |
| MINNESOTA, US 70         | MINNESOTA, US 56         | NETHERLANDS 60           | UNITED STATES 57         | LATVIA 66                | LATVIA 62                |
| ENGLAND 69               | NETHERLANDS 55           | JAPAN 60                 | JAPAN 56                 | ENGLAND 62               | NETHERLANDS 61           |
| LATVIA 68                | HUNGARY 53               | UNITED STATES 59         | NETHERLANDS 53           | MINNESOTA, US 59         | AUSTRALIA 55             |
| QUEBEC, CANADA 67        | ENGLAND 52               | QUEBEC, CANADA 57        | ITALY 50                 | CZECH REPUBLIC 57        | ENGLAND 54               |
| HUNGARY 66               | UNITED STATES 51         | AUSTRALIA 55             | LATVIA 49                | HUNGARY 57               | AUSTRIA 53               |
| UNITED STATES 66         | AUSTRIA 48               | LATVIA 52                | QUEBEC, CANADA 44        | AUSTRIA 57               | QUEBEC, CANADA 53        |
| AUSTRIA 64               | QUEBEC, CANADA 48        | NEW ZEALAND 50           | AUSTRALIA 43             | AUSTRALIA 54             | UNITED STATES 52         |
| ALBERTA, CANADA 62       | CZECH REPUBLIC 47        | ONTARIO, CANADA 50       | NEW ZEALAND 40           | SLOVENIA 51              | ONTARIO, CANADA 50       |
| AUSTRALIA 62             | SLOVENIA 47              | ALBERTA, CANADA 49       | International Average 38 | SCOTLAND 50              | HUNGARY 48               |
| ONTARIO, CANADA 62       | ITALY 47                 | SCOTLAND 49              | ONTARIO, CANADA 35       | UNITED STATES 49         | ALBERTA, CANADA 47       |
| SCOTLAND 60              | International Average 44 | ITALY 47                 | ALBERTA, CANADA 34       | NEW ZEALAND 49           | International Average 46 |
| CZECH REPUBLIC 60        | AUSTRALIA 43             | HUNGARY 44               | AUSTRIA 34               | ALBERTA, CANADA 49       | ITALY 44                 |
| ITALY 59                 | ONTARIO, CANADA 42       | International Average 42 | HUNGARY 34               | QUEBEC, CANADA 49        | CZECH REPUBLIC 43        |
| NEW ZEALAND 57           | ALBERTA, CANADA 42       | SLOVENIA 41              | SCOTLAND 33              | ONTARIO, CANADA 49       | SLOVENIA 42              |
| SLOVENIA 56              | SCOTLAND 40              | AUSTRIA 39               | NORWAY 29                | International Average 46 | NORWAY 40                |
| International Average 56 | NEW ZEALAND 38           | NORWAY 38                | SLOVENIA 25              | ITALY 45                 | SCOTLAND 40              |
| NORWAY 53                | NORWAY 36                | CZECH REPUBLIC 27        | CZECH REPUBLIC 20        | NORWAY 44                | NEW ZEALAND 38           |
| IRAN, ISLAMIC REP. OF 39 | IRAN, ISLAMIC REP. OF 27 | IRAN, ISLAMIC REP. OF 24 | IRAN, ISLAMIC REP. OF 16 | IRAN, ISLAMIC REP. OF 23 | IRAN, ISLAMIC REP. OF 30 |
| KUWAIT 37                | KUWAIT 17                | KUWAIT 19                | KUWAIT 13                | KUWAIT 14                | KUWAIT 21                |

| Geometry: Position & Shapes | Symmetry, Congruence & Similarity | Proportionality          | Patterns, Relations, & Functions | Equations & Formulas     | Data Representation, Probability & Statistics |
|-----------------------------|-----------------------------------|--------------------------|----------------------------------|--------------------------|---|
| HONG KONG SAR 78            | HONG KONG SAR 83                  | HONG KONG SAR 75         | SINGAPORE 71                     | HONG KONG SAR 73         | HONG KONG SAR 85                              |
| SINGAPORE 71                | SINGAPORE 81                      | SINGAPORE 69             | HONG KONG SAR 71                 | SINGAPORE 69             | SINGAPORE 83                                  |
| JAPAN 70                    | ENGLAND 73                        | JAPAN 64                 | JAPAN 65                         | JAPAN 68                 | JAPAN 82                                      |
| MINNESOTA, US 67            | MINNESOTA, US 72                  | LATVIA 59                | MINNESOTA, US 62                 | MINNESOTA, US 62         | MINNESOTA, US 77                              |
| ENGLAND 64                  | ONTARIO, CANADA 67                | NETHERLANDS 57           | ENGLAND 59                       | HUNGARY 59               | ENGLAND 75                                    |
| AUSTRALIA 61                | JAPAN 65                          | MINNESOTA, US 56         | LATVIA 59                        | UNITED STATES 58         | UNITED STATES 74                              |
| LATVIA 61                   | AUSTRALIA 65                      | ENGLAND 55               | UNITED STATES 57                 | LATVIA 57                | ONTARIO, CANADA 74                            |
| QUEBEC, CANADA 61           | UNITED STATES 64                  | ONTARIO, CANADA 54       | NETHERLANDS 56                   | ENGLAND 56               | NETHERLANDS 73                                |
| ONTARIO, CANADA 60          | SLOVENIA 62                       | UNITED STATES 52         | HUNGARY 55                       | ITALY 53                 | ALBERTA, CANADA 72                            |
| UNITED STATES 59            | SCOTLAND 61                       | AUSTRALIA 52             | ONTARIO, CANADA 53               | NETHERLANDS 51           | LATVIA 71                                     |
| NETHERLANDS 57              | ITALY 60                          | ALBERTA, CANADA 48       | ITALY 52                         | AUSTRALIA 48             | AUSTRALIA 70                                  |
| SLOVENIA 57                 | NEW ZEALAND 59                    | QUEBEC, CANADA 47        | AUSTRALIA 51                     | QUEBEC, CANADA 47        | QUEBEC, CANADA 69                             |
| AUSTRIA 56                  | HUNGARY 58                        | HUNGARY 46               | ALBERTA, CANADA 51               | ONTARIO, CANADA 46       | SCOTLAND 66                                   |
| HUNGARY 55                  | NETHERLANDS 57                    | SLOVENIA 45              | QUEBEC, CANADA 51                | ALBERTA, CANADA 46       | SLOVENIA 65                                   |
| ALBERTA, CANADA 55          | ALBERTA, CANADA 57                | ITALY 44                 | NEW ZEALAND 48                   | CZECH REPUBLIC 46        | NEW ZEALAND 65                                |
| ITALY 54                    | LATVIA 56                         | NEW ZEALAND 44           | AUSTRIA 48                       | International Average 46 | AUSTRIA 63                                    |
| SCOTLAND 52                 | QUEBEC, CANADA 56                 | SCOTLAND 42              | SLOVENIA 47                      | SLOVENIA 45              | ITALY 62                                      |
| NEW ZEALAND 51              | AUSTRIA 52                        | International Average 42 | SCOTLAND 46                      | AUSTRIA 45               | HUNGARY 61                                    |
| CZECH REPUBLIC 50           | International Average 49          | CZECH REPUBLIC 40        | CZECH REPUBLIC 46                | SCOTLAND 44              | CZECH REPUBLIC 58                             |
| NORWAY 49                   | CZECH REPUBLIC 48                 | AUSTRIA 39               | International Average 46         | NEW ZEALAND 44           | NORWAY 57                                     |
| International Average 49    | NORWAY 47                         | NORWAY 37                | NORWAY 42                        | NORWAY 39                | International Average 56                      |
| IRAN, ISLAMIC REP. OF 37    | IRAN, ISLAMIC REP. OF 37          | IRAN, ISLAMIC REP. OF 27 | IRAN, ISLAMIC REP. OF 26         | IRAN, ISLAMIC REP. OF 32 | IRAN, ISLAMIC REP. OF 34                      |
| KUWAIT 20                   | KUWAIT 18                         | KUWAIT 14                | KUWAIT 17                        | KUWAIT 21                | KUWAIT 22                                     |

|                                     |
|-------------------------------------|
| Significantly higher than MN        |
| Not Statistically Different from MN |
| Significantly lower than MN         |



Display 3: Grade 8 Mathematics Topics

| Whole Numbers            | Common Fractions         | Decimal Fractions & Percents | Relations of Fractions   | Estimating Quantity & Size | Rounding                 |
|--------------------------|--------------------------|------------------------------|--------------------------|----------------------------|--------------------------|
| SINGAPORE 72             | SINGAPORE 72             | SINGAPORE 78                 | KOREA, REP. OF 79        | KOREA, REP. OF 67          | SINGAPORE 63             |
| KOREA, REP. OF 71        | KOREA, REP. OF 68        | KOREA, REP. OF 72            | SINGAPORE 79             | MINNESOTA, US 86           | HONG KONG SAR 62         |
| HONG KONG SAR 68         | HONG KONG SAR 64         | HONG KONG SAR 71             | HONG KONG SAR 74         | JAPAN 64                   | KOREA, REP. OF 55        |
| JAPAN 66                 | JAPAN 60                 | JAPAN 69                     | JAPAN 67                 | SINGAPORE 63               | MINNESOTA, US 60         |
| MINNESOTA, US 88         | QUEBEC, CANADA 49        | QUEBEC, CANADA 69            | MINNESOTA, US 84         | UNITED STATES 80           | JAPAN 49                 |
| ONTARIO, CANADA 62       | RUSSIAN FEDERATION 46    | MINNESOTA, US 87             | QUEBEC, CANADA 59        | HUNGARY 60                 | UNITED STATES 48         |
| QUEBEC, CANADA 60        | HUNGARY 46               | SWEDEN 65                    | ONTARIO, CANADA 57       | SLOVENIA 60                | QUEBEC, CANADA 42        |
| UNITED STATES 68         | ONTARIO, CANADA 45       | ONTARIO, CANADA 64           | UNITED STATES 68         | ENGLAND 59                 | ONTARIO, CANADA 42       |
| ENGLAND 58               | MINNESOTA, US 46         | ENGLAND 62                   | RUSSIAN FEDERATION 55    | ONTARIO, CANADA 59         | HUNGARY 40               |
| CZECH REPUBLIC 57        | CZECH REPUBLIC 44        | LITHUANIA 62                 | HUNGARY 54               | HONG KONG SAR 58           | SWEDEN 40                |
| HUNGARY 57               | ITALY 43                 | HUNGARY 62                   | SWEDEN 53                | AUSTRALIA 57               | ENGLAND 39               |
| AUSTRALIA 56             | SWEDEN 42                | CZECH REPUBLIC 62            | LITHUANIA 52             | QUEBEC, CANADA 57          | LITHUANIA 38             |
| SLOVENIA 55              | ENGLAND 42               | UNITED STATES 80             | CZECH REPUBLIC 51        | SWEDEN 54                  | CZECH REPUBLIC 38        |
| SWEDEN 55                | LITHUANIA 42             | AUSTRALIA 58                 | AUSTRALIA 50             | SCOTLAND 54                | RUSSIAN FEDERATION 37    |
| RUSSIAN FEDERATION 54    | SLOVENIA 40              | RUSSIAN FEDERATION 57        | ENGLAND 48               | CZECH REPUBLIC 54          | NORWAY 35                |
| SCOTLAND 53              | AUSTRALIA 40             | SCOTLAND 57                  | SLOVENIA 48              | ITALY 51                   | AUSTRALIA 35             |
| NORWAY 51                | UNITED STATES 40         | NORWAY 57                    | NORWAY 46                | LITHUANIA 51               | SLOVENIA 34              |
| LITHUANIA 51             | CYPRUS 37                | SLOVENIA 57                  | ISRAEL 46                | RUSSIAN FEDERATION 51      | BULGARIA 33              |
| ITALY 50                 | ISRAEL 37                | ITALY 52                     | BULGARIA 46              | NORWAY 51                  | SCOTLAND 31              |
| THAILAND 43              | SCOTLAND 36              | ISRAEL 48                    | International Average 44 | CYPRUS 41                  | International Average 29 |
| ISRAEL 43                | NORWAY 36                | BULGARIA 48                  | SCOTLAND 43              | International Average 40   | ITALY 28                 |
| BULGARIA 42              | International Average 35 | CYPRUS 47                    | ITALY 43                 | THAILAND 40                | ISRAEL 28                |
| CYPRUS 42                | ROMANIA 35               | International Average 46     | CYPRUS 42                | BULGARIA 40                | THAILAND 28              |
| International Average 41 | BULGARIA 34              | ROMANIA 45                   | ROMANIA 42               | ROMANIA 40                 | ROMANIA 27               |
| ROMANIA 38               | THAILAND 31              | THAILAND 40                  | THAILAND 36              | ISRAEL 39                  | CYPRUS 27                |
| IRAN, ISLAMIC REP. OF 29 | IRAN, ISLAMIC REP. OF 27 | IRAN, ISLAMIC REP. OF 30     | IRAN, ISLAMIC REP. OF 31 | COLOMBIA 35                | IRAN, ISLAMIC REP. OF 15 |
| COLOMBIA 27              | COLOMBIA 19              | COLOMBIA 24                  | KUWAIT 25                | KUWAIT 25                  | COLOMBIA 9               |
| KUWAIT 20                | KUWAIT 19                | KUWAIT 21                    | COLOMBIA 19              | IRAN, ISLAMIC REP. OF 24   | KUWAIT 9                 |

| Measurement Units        | Perimeter, Area & Volume | 2-D Geometry             | Polygons & Circles       | 3-D Geometry & Transformations | Proportionality Concepts |
|--------------------------|--------------------------|--------------------------|--------------------------|--------------------------------|--------------------------|
| SINGAPORE 73             | SINGAPORE 70             | KOREA, REP. OF 74        | KOREA, REP. OF 68        | JAPAN 73                       | SINGAPORE 80             |
| KOREA, REP. OF 69        | HONG KONG SAR 66         | JAPAN 72                 | SINGAPORE 68             | KOREA, REP. OF 72              | KOREA, REP. OF 76        |
| HONG KONG SAR 67         | KOREA, REP. OF 64        | HONG KONG SAR 67         | HONG KONG SAR 66         | SINGAPORE 71                   | HONG KONG SAR 65         |
| JAPAN 67                 | JAPAN 60                 | SINGAPORE 66             | JAPAN 65                 | HONG KONG SAR 71               | JAPAN 62                 |
| QUEBEC, CANADA 58        | QUEBEC, CANADA 48        | QUEBEC, CANADA 52        | RUSSIAN FEDERATION 48    | ENGLAND 65                     | RUSSIAN FEDERATION 48    |
| ENGLAND 57               | MINNESOTA, US 48         | SLOVENIA 49              | QUEBEC, CANADA 48        | ONTARIO, CANADA 63             | ONTARIO, CANADA 47       |
| MINNESOTA, US 67         | LITHUANIA 47             | ENGLAND 48               | HUNGARY 47               | QUEBEC, CANADA 61              | MINNESOTA, US 47         |
| SLOVENIA 53              | ONTARIO, CANADA 46       | HUNGARY 48               | ENGLAND 45               | HUNGARY 60                     | ENGLAND 46               |
| CZECH REPUBLIC 53        | ENGLAND 45               | RUSSIAN FEDERATION 48    | LITHUANIA 44             | LITHUANIA 60                   | QUEBEC, CANADA 46        |
| HUNGARY 53               | HUNGARY 44               | MINNESOTA, US 46         | ITALY 43                 | AUSTRALIA 59                   | HUNGARY 45               |
| SWEDEN 53                | RUSSIAN FEDERATION 44    | CZECH REPUBLIC 45        | CZECH REPUBLIC 42        | MINNESOTA, US 68               | CZECH REPUBLIC 44        |
| SCOTLAND 52              | ITALY 43                 | ONTARIO, CANADA 44       | SLOVENIA 42              | SCOTLAND 58                    | UNITED STATES 44         |
| UNITED STATES 51         | ROMANIA 42               | LITHUANIA 43             | ONTARIO, CANADA 42       | CZECH REPUBLIC 55              | BULGARIA 42              |
| ONTARIO, CANADA 51       | CZECH REPUBLIC 41        | BULGARIA 43              | MINNESOTA, US 42         | SLOVENIA 55                    | AUSTRALIA 41             |
| AUSTRALIA 49             | UNITED STATES 40         | SCOTLAND 41              | ROMANIA 41               | UNITED STATES 53               | SCOTLAND 40              |
| RUSSIAN FEDERATION 49    | SLOVENIA 39              | AUSTRALIA 40             | BULGARIA 40              | RUSSIAN FEDERATION 53          | CYPRUS 39                |
| LITHUANIA 48             | AUSTRALIA 38             | UNITED STATES 39         | SWEDEN 40                | ITALY 49                       | LITHUANIA 38             |
| NORWAY 45                | SWEDEN 38                | SWEDEN 39                | CYPRUS 39                | SWEDEN 47                      | International Average 37 |
| CYPRUS 40                | CYPRUS 37                | ITALY 39                 | International Average 38 | NORWAY 46                      | THAILAND 37              |
| ITALY 40                 | BULGARIA 37              | ISRAEL 38                | SCOTLAND 37              | BULGARIA 42                    | ITALY 36                 |
| THAILAND 40              | SCOTLAND 35              | ROMANIA 37               | ISRAEL 37                | International Average 42       | ROMANIA 36               |
| International Average 38 | International Average 35 | THAILAND 37              | AUSTRALIA 37             | CYPRUS 40                      | SLOVENIA 33              |
| ISRAEL 38                | NORWAY 33                | CYPRUS 37                | UNITED STATES 37         | ROMANIA 40                     | ISRAEL 33                |
| BULGARIA 37              | ISRAEL 32                | NORWAY 36                | THAILAND 36              | THAILAND 39                    | NORWAY 31                |
| ROMANIA 34               | THAILAND 29              | IRAN, ISLAMIC REP. OF 32 | NORWAY 35                | ISRAEL 35                      | IRAN, ISLAMIC REP. OF 28 |
| COLOMBIA 25              | IRAN, ISLAMIC REP. OF 25 | KUWAIT 27                | IRAN, ISLAMIC REP. OF 30 | IRAN, ISLAMIC REP. OF 33       | KUWAIT 28                |
| IRAN, ISLAMIC REP. OF 24 | KUWAIT 19                | COLOMBIA 20              | KUWAIT 23                | KUWAIT 27                      | SWEDEN 25                |
| KUWAIT 22                | COLOMBIA 18              | International Average 39 | COLOMBIA 20              | COLOMBIA 26                    | COLOMBIA 20              |

Significantly higher than MN  
 Not Statistically Different from MN  
 Significantly lower than MN

Display 3: Grade 8 Mathematics Topics

| Proportionality Problems |    | Patterns, Relations, & Functions |    | Equations & Formulas  |    | Data Representation & Analysis |    | Uncertainty & Probability |    |
|--------------------------|----|----------------------------------|----|-----------------------|----|--------------------------------|----|---------------------------|----|
| KOREA, REP. OF           | 69 | KOREA, REP. OF                   | 66 | KOREA, REP. OF        | 70 | KOREA, REP. OF                 | 72 | KOREA, REP. OF            | 87 |
| SINGAPORE                | 69 | SINGAPORE                        | 64 | SINGAPORE             | 68 | SINGAPORE                      | 72 | JAPAN                     | 76 |
| HONG KONG SAR            | 63 | JAPAN                            | 62 | HONG KONG SAR         | 65 | JAPAN                          | 71 | MINNESOTA, US             | 76 |
| JAPAN                    | 54 | HONG KONG SAR                    | 57 | JAPAN                 | 61 | MINNESOTA, US                  | 87 | SINGAPORE                 | 72 |
| QUEBEC, CANADA           | 50 | MINNESOTA, US                    | 48 | RUSSIAN FEDERATION    | 51 | HONG KONG SAR                  | 66 | ENGLAND                   | 72 |
| ENGLAND                  | 49 | QUEBEC, CANADA                   | 46 | MINNESOTA, US         | 48 | ENGLAND                        | 62 | ONTARIO, CANADA           | 71 |
| MINNESOTA, US            | 48 | HUNGARY                          | 45 | QUEBEC, CANADA        | 46 | ONTARIO, CANADA                | 62 | QUEBEC, CANADA            | 71 |
| RUSSIAN FEDERATION       | 44 | ENGLAND                          | 45 | HUNGARY               | 46 | QUEBEC, CANADA                 | 60 | HONG KONG SAR             | 69 |
| ONTARIO, CANADA          | 42 | ONTARIO, CANADA                  | 44 | UNITED STATES         | 44 | UNITED STATES                  | 68 | AUSTRALIA                 | 67 |
| HUNGARY                  | 42 | SLOVENIA                         | 41 | ROMANIA               | 43 | HUNGARY                        | 58 | UNITED STATES             | 87 |
| LITHUANIA                | 42 | RUSSIAN FEDERATION               | 41 | ENGLAND               | 42 | SWEDEN                         | 58 | LITHUANIA                 | 66 |
| SWEDEN                   | 41 | UNITED STATES                    | 41 | LITHUANIA             | 42 | LITHUANIA                      | 57 | SWEDEN                    | 62 |
| UNITED STATES            | 41 | AUSTRALIA                        | 41 | BULGARIA              | 42 | AUSTRALIA                      | 56 | SCOTLAND                  | 60 |
| AUSTRALIA                | 41 | SCOTLAND                         | 39 | SLOVENIA              | 41 | SLOVENIA                       | 55 | NORWAY                    | 58 |
| SLOVENIA                 | 40 | CZECH REPUBLIC                   | 39 | ONTARIO, CANADA       | 41 | SCOTLAND                       | 54 | HUNGARY                   | 58 |
| ROMANIA                  | 39 | LITHUANIA                        | 36 | CZECH REPUBLIC        | 39 | CZECH REPUBLIC                 | 54 | CZECH REPUBLIC            | 57 |
| SCOTLAND                 | 38 | BULGARIA                         | 35 | ISRAEL                | 39 | NORWAY                         | 52 | SLOVENIA                  | 57 |
| CZECH REPUBLIC           | 38 | SWEDEN                           | 35 | CYPRUS                | 38 | RUSSIAN FEDERATION             | 48 | ITALY                     | 57 |
| CYPRUS                   | 38 | ITALY                            | 34 | ITALY                 | 36 | ITALY                          | 48 | RUSSIAN FEDERATION        | 55 |
| ISRAEL                   | 36 | ROMANIA                          | 34 | AUSTRALIA             | 36 | ISRAEL                         | 44 | CYPRUS                    | 52 |
| BULGARIA                 | 35 | ISRAEL                           | 34 | International Average | 36 | CYPRUS                         | 41 | ISRAEL                    | 51 |
| International Average    | 34 | CYPRUS                           | 33 | SCOTLAND              | 35 | International Average          | 41 | International Average     | 47 |
| NORWAY                   | 32 | International Average            | 32 | SWEDEN                | 33 | THAILAND                       | 40 | BULGARIA                  | 46 |
| THAILAND                 | 30 | NORWAY                           | 32 | THAILAND              | 29 | BULGARIA                       | 37 | ROMANIA                   | 43 |
| ITALY                    | 30 | THAILAND                         | 30 | NORWAY                | 26 | ROMANIA                        | 35 | THAILAND                  | 42 |
| IRAN, ISLAMIC REP. OF    | 24 | IRAN, ISLAMIC REP. OF            | 24 | IRAN, ISLAMIC REP. OF | 25 | IRAN, ISLAMIC REP. OF          | 28 | IRAN, ISLAMIC REP. OF     | 39 |
| COLOMBIA                 | 20 | COLOMBIA                         | 20 | COLOMBIA              | 20 | COLOMBIA                       | 28 | COLOMBIA                  | 32 |
| KUWAIT                   | 16 | KUWAIT                           | 14 | KUWAIT                | 18 | KUWAIT                         | 22 | KUWAIT                    | 26 |

## **Content – Curriculum, Standards and Textbooks**

What are the characteristics of a coherent and focused curriculum? Can these characteristics be identified or measured? We believe that a coherent curriculum introduces and develops topics in a logical sequence.

Different topics ‘fit’ together as part of an integrated, systematic whole, both within a grade level and from grade to grade. Simple concepts are first introduced within simple topics. Topics are developed fully by gradually moving to more complex concepts. Once a topic has been fully developed, it is excluded from the curriculum and other, more complex topics are introduced.

A focused curriculum is one that intends a carefully selected and relatively small number of topics, especially in the early grades. The idea is that less is more, in that if fewer topics are included in the curriculum, the few can be addressed in greater depth. The concepts related to them can be developed completely so that students fully understand them. Such an approach facilitates the process of building a strong foundation in mathematics while advancing on to new and more complex topics in succeeding years of study.

One model of a coherent curriculum for mathematics is depicted in the display that follows. It is a matrix that depicts a composite of mathematics content areas of the top achieving countries (TAC) intended for grades one through eight according to results from the Third International Mathematics and Science Study (TIMSS), completed in 1995.

Thirty-two topics are identified in rows that are listed in the left column. The remaining columns identify the first eight grades. Our matrix has 256 cells (8 x 32). There are 99 shaded cells that identify the grades in which topics are included in the mathematics curricula in more than half of the TAC (four out of six countries).

Thus the shaded cells, representing topic-grade combinations, can be referred to as “coherence cells”. The display lists topics in somewhat the same sequence suggested by results from the TAC curricular studies. The sequence of the major topics can be thought of as in a hierarchical structure that concurrently establishes a logical sequence for introducing these topics across the grades. (Figure 29)

By overlaying the curriculum intended according to the Minnesota standards on the appropriate silhouetted region, our model of a coherent and focused curriculum, we have a sense for the extent of agreement with our models. Whether examining the mathematics or science matrix, the cells within the matrix fall into three groups:

- 1) Cells that match the shaded area, displaying agreement with the ideal scenario of coherence as defined by our model.
- 2) Cells that are located in the grid in grades before those defined by the shaded region – these cells indicate topics that are covered earlier than that suggested by the ideal scenario of our model.
- 3) Cells that are located in the grid in grades after those defined by the shaded region – these cells indicate that topics are introduced or covered beyond the time that is recommended by our model.



### Mathematics Topics Intended at Each Grade in the state of Minnesota

| Topic  | Grade |   |   |   |   |   |   |   |
|--|-------|---|---|---|---|---|---|---|
|  | 1     | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| Whole Number: Meaning                          | •     | • | • | • |   |   |   |   |
| Whole Number: Operations                       | •     | • | • | • | • |   |   |   |
| Measurement Units                              | •     | • | • | • | • | • | • | • |
| Common Fractions                               | •     | • | • | • | • | • | • |   |
| Equations & Formulas                           |       |   | • | • | • | • | • | • |
| Data Representation & Analysis                 | •     | • | • | • | • | • | • | • |
| 2-D Geometry: Basics                           |       |   | • | • | • | • | • |   |
| 2-D Geometry: Polygons & Circles               | •     | • | • | • | • | • | • | • |
| Measurement: Perimeter, Area & Volume          |       |   | • | • | • | • | • | • |
| Rounding & Significant Figures                 |       |   |   | • | • | • |   |   |
| Estimating Computations                        |       | • |   | • | • | • | • | • |
| Whole Numbers: Properties of Operations        |       | • | • | • |   | • | • | • |
| Estimating Quantity & Size                     |       |   |   |   |   |   |   |   |
| Decimal Fractions                              |       | • | • | • | • | • |   |   |
| Relation of Common & Decimal Fractions         |       |   |   |   |   |   | • |   |
| Properties of Common & Decimal Fractions       |       |   |   |   |   |   |   |   |
| Percentages                                    |       |   |   |   | • | • | • | • |
| Proportionality Concepts                       |       |   |   |   |   |   |   |   |
| Proportionality Problems                       |       |   |   |   |   |   | • | • |
| 2-D Geometry: Coordinate Geometry              |       |   |   |   |   | • | • | • |
| Geometry: Transformations                      | •     | • | • |   | • | • | • | • |
| Negative Numbers, Integers, & Their Properties |       |   |   |   | • | • |   |   |
| Number Theory                                  | •     | • |   |   |   | • |   |   |
| Exponents, Roots & Radicals                    |       |   |   |   |   |   | • | • |
| Exponents & Orders of Magnitude                |       |   |   |   |   |   | • | • |
| Measurement: Estimation & Errors               | •     | • |   |   |   |   |   |   |
| Constructions Using Straightedge & Compass     |       |   |   |   |   | • |   |   |
| 3-D Geometry                                   | •     | • | • | • | • | • | • | • |
| Geometry: Congruence & Similarity              |       |   |   | • |   |   |   |   |
| Rational Numbers & Their Properties            |       |   |   |   |   | • | • | • |
| Patterns, Relations & Functions                |       | • | • | • | • |   | • | • |
| Proportionality: Slope & Trigonometry          |       |   |   |   |   |   | • |   |

Figure 29

Observations for mathematics follow:  
Across the first four grades, Minnesota intended to cover most of the same topics that were intended by the TAC. All topics that were intended by the TAC were intended in the Minnesota standards in

grades one through three. Only two topics were not intended in fourth grade that were intended by the TAC: Estimating Quantity and Size; Relation of Common and Decimal Fractions.

The matrix identifies thirty-nine cases across grades one through seven where Minnesota intended to cover topics earlier than the grade first suggested by the coherence model. Several topics were intended not only earlier but also in two or more grades prior to what the coherence model suggests. The topics most frequently covered early were: Common and Decimal Fractions; Data Representation & Analysis; 2-D Geometry, Polygons & Circles; Whole Numbers, Properties of Operations; Transformations; 3-D Geometry; and Patterns, Relations & Functions.

The number of topics intended to be covered early in grades one through three is of particular concern. When teachers must dedicate classroom time teaching topics before their time as suggested by the coherence model they have less time to develop the concepts related to the topics that are considered more essential at the early grades: Whole Numbers, Meaning and Operations; and Measurement Units.

This is particularly extreme in grade two. Out of the thirty-two topics that are considered in the matrix, Minnesota intended to cover eleven more topics than the three suggested by the TAC composite.

Moving across the matrix to the higher grades, there are several topics in each of grades five through eight that were intended by the TAC but not the Minnesota standards. These topics fall into the three categories: those that are

not covered in any of the eight grades (three topics); those that are covered in earlier grades; and topics that were intended in grades later than suggested by the model.

One of the topics never intended, Estimating Quantity & Size, was mentioned above as part of the discussion related to grade four. The other two topics that were not intended in grades one through eight are: Properties of Common & Decimal Fractions; and Proportionality Concepts.

Other topics of particular concern that were not intended according to the suggested model are: Relation of Common & /Decimal Fractions; Proportionality Problems; Coordinate Geometry; Proportionality, Slope & Trigonometry. These topics are important to laying a foundation for more complex content that will be introduced in later high school courses.

Taken together these gaps in intended topic coverage are noteworthy because concepts associated with these topics must be developed fully in grades five through eight to ensure that students have the foundation that they need to understand even more complex content related to algebra, geometry, trigonometry and beyond.

Figures 29a and 29b show how the mathematics topic focus in MN compares to the rest of the US in 2007 and how it has changed from 1995.



## Comparing MN and the US: Grade 4 Mathematics

| Topic   | 1995 | 2007 |
|---|------|------|
| Meaning of Whole Numbers                      |      |      |
| Whole Number Operations                       |      |      |
| Common Fractions                              |      |      |
| Decimal Fractions                             |      |      |
| Measurement Units                             |      |      |
| Perimeter, Area & Volume                      |      |      |
| Geometry: Position & Shapes                   |      |      |
| Symmetry, Congruence & Similarity             |      |      |
| Proportionality                               |      |      |
| Patterns, Relations, & Functions              |      |      |
| Equations & Formulas                          |      |      |
| Data Representation, Probability & Statistics |      |      |

MN > US
  MN = US
  MN < US

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Figure 29a

## Comparing MN and the US: Grade 8 Mathematics

| Topic                            | 1995 | 2007 |
|----------------------------------|------|------|
| Whole Numbers                    |      |      |
| Common Fractions                 |      |      |
| Decimal Fractions & Percents     |      |      |
| Relations of Fractions           |      |      |
| Estimating Quantity & Size       |      |      |
| Rounding                         |      |      |
| Measurement Units                |      |      |
| Perimeter, Area & Volume         |      |      |
| 2-D Geometry                     |      |      |
| Polygons & Circles               |      |      |
| 3-D Geometry & Transformations   |      |      |
| Proportionality Concepts         |      |      |
| Proportionality Problems         |      |      |
| Patterns, Relations, & Functions |      |      |
| Equations & Formulas             |      |      |
| Data Representation & Analysis   |      |      |
| Uncertainty & Probability        |      |      |

MN > US
  MN = US
  MN < US

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Figure 29b

## MINNESOTA STUDENTS' PERFORMANCE IN BROAD AREAS OF SCIENCE: 2007 INTERNATIONAL COMPARISONS

TIMSS test items were coded into 15 broad categories for Grade 4 science and 17 categories for grade 8 science, the same categories used in the 1995 analysis.

### GRADE 4 SCIENCE

- Only students in Singapore scored significantly higher overall than Minnesota students.
- Singapore scored higher on seven of the broad science categories displayed.
- Japan on three broad science categories-Human Biology and Health; Energy and Physical Processes; and Physical and Chemical Changes.
- Netherlands on one broad science category-Human Biology and Health.
- MN students maintained their relatively high level of performance in science at a time when the requirements of No Child Left Behind led elementary schools to heavily emphasize reading and math instruction
- MN students scored significantly higher than the U.S. students in one area of science - Forces and motion.
- Although MN students scored higher than the US students in all but one other broad category, the differences were not statistically significant. (Figures 30 and 31)

| Display 2: Grade 4 Science Topics |    |                       |    |                       |    |                       |    |                       |    |
|-----------------------------------|----|-----------------------|----|-----------------------|----|-----------------------|----|-----------------------|----|
| Earth Features                    |    | Earth Processes       |    | Earth in the Universe |    | Plants & Animals      |    | Organs & Tissues      |    |
| MINNESOTA, US                     | 70 | ALBERTA, CANADA       | 70 | LATVIA                | 66 | SINGAPORE             | 70 | HUNGARY               | 63 |
| HONG KONG SAR                     | 66 | JAPAN                 | 70 | ENGLAND               | 66 | ITALY                 | 63 | ITALY                 | 63 |
| UNITED STATES                     | 64 | MINNESOTA, US         | 67 | SINGAPORE             | 66 | MINNESOTA, US         | 62 | NETHERLANDS           | 62 |
| SINGAPORE                         | 64 | ONTARIO, CANADA       | 66 | HONG KONG SAR         | 63 | ALBERTA, CANADA       | 61 | AUSTRIA               | 61 |
| ALBERTA, CANADA                   | 64 | ENGLAND               | 65 | MINNESOTA, US         | 62 | UNITED STATES         | 61 | SLOVENIA              | 60 |
| ENGLAND                           | 63 | UNITED STATES         | 65 | UNITED STATES         | 61 | ENGLAND               | 60 | SINGAPORE             | 60 |
| JAPAN                             | 63 | ITALY                 | 64 | ALBERTA, CANADA       | 60 | ONTARIO, CANADA       | 60 | MINNESOTA, US         | 60 |
| AUSTRIA                           | 62 | HONG KONG SAR         | 64 | AUSTRALIA             | 60 | LATVIA                | 60 | LATVIA                | 60 |
| AUSTRALIA                         | 60 | AUSTRIA               | 64 | ONTARIO, CANADA       | 58 | HUNGARY               | 60 | ENGLAND               | 59 |
| ONTARIO, CANADA                   | 60 | AUSTRALIA             | 64 | AUSTRIA               | 58 | HONG KONG SAR         | 59 | ONTARIO, CANADA       | 58 |
| NETHERLANDS                       | 60 | NETHERLANDS           | 63 | SLOVENIA              | 56 | AUSTRALIA             | 59 | UNITED STATES         | 58 |
| LATVIA                            | 60 | QUEBEC, CANADA        | 61 | HUNGARY               | 56 | NETHERLANDS           | 58 | HONG KONG SAR         | 58 |
| ITALY                             | 59 | HUNGARY               | 60 | NETHERLANDS           | 55 | CZECH REPUBLIC        | 57 | ALBERTA, CANADA       | 58 |
| HUNGARY                           | 58 | SINGAPORE             | 60 | NORWAY                | 55 | AUSTRIA               | 57 | CZECH REPUBLIC        | 56 |
| SCOTLAND                          | 57 | CZECH REPUBLIC        | 60 | NEW ZEALAND           | 55 | JAPAN                 | 56 | QUEBEC, CANADA        | 54 |
| NEW ZEALAND                       | 57 | NEW ZEALAND           | 59 | QUEBEC, CANADA        | 55 | QUEBEC, CANADA        | 55 | AUSTRALIA             | 53 |
| SLOVENIA                          | 56 | LATVIA                | 58 | ITALY                 | 54 | NEW ZEALAND           | 54 | JAPAN                 | 53 |
| NORWAY                            | 54 | SCOTLAND              | 58 | SCOTLAND              | 54 | SLOVENIA              | 54 | SCOTLAND              | 51 |
| QUEBEC, CANADA                    | 53 | SLOVENIA              | 57 | JAPAN                 | 54 | SCOTLAND              | 54 | NEW ZEALAND           | 50 |
| International Average             | 51 | International Average | 51 | CZECH REPUBLIC        | 53 | International Average | 50 | NORWAY                | 50 |
| CZECH REPUBLIC                    | 50 | NORWAY                | 51 | International Average | 50 | NORWAY                | 50 | International Average | 49 |
| IRAN, ISLAMIC REP. OF             | 37 | IRAN, ISLAMIC REP. OF | 34 | IRAN, ISLAMIC REP. OF | 40 | IRAN, ISLAMIC REP. OF | 42 | IRAN, ISLAMIC REP. OF | 37 |
| KUWAIT                            | 30 | KUWAIT                | 32 | KUWAIT                | 27 | KUWAIT                | 33 | KUWAIT                | 28 |
| TUNISIA                           | 20 | TUNISIA               | 27 | TUNISIA               | 23 | TUNISIA               | 26 | TUNISIA               | 24 |

| Life Processes & Function |    | Life Cycles & Genetics |    | Interactions of Living Things |    | Human Biology and Health |    | Matter                |    |
|---------------------------|----|------------------------|----|-------------------------------|----|--------------------------|----|-----------------------|----|
| SINGAPORE                 | 82 | SINGAPORE              | 62 | ITALY                         | 71 | JAPAN                    | 65 | SINGAPORE             | 72 |
| HONG KONG SAR             | 63 | AUSTRIA                | 58 | AUSTRIA                       | 70 | SINGAPORE                | 64 | HONG KONG SAR         | 67 |
| ONTARIO, CANADA           | 60 | CZECH REPUBLIC         | 56 | SINGAPORE                     | 69 | NETHERLANDS              | 63 | JAPAN                 | 65 |
| ITALY                     | 59 | HUNGARY                | 56 | NETHERLANDS                   | 69 | HONG KONG SAR            | 61 | LATVIA                | 64 |
| UNITED STATES             | 58 | MINNESOTA, US          | 55 | MINNESOTA, US                 | 68 | ITALY                    | 61 | MINNESOTA, US         | 61 |
| ALBERTA, CANADA           | 57 | ITALY                  | 55 | HUNGARY                       | 68 | HUNGARY                  | 60 | ITALY                 | 61 |
| ENGLAND                   | 56 | LATVIA                 | 54 | LATVIA                        | 66 | QUEBEC, CANADA           | 60 | AUSTRIA               | 59 |
| MINNESOTA, US             | 55 | ALBERTA, CANADA        | 53 | ALBERTA, CANADA               | 66 | LATVIA                   | 59 | ENGLAND               | 59 |
| JAPAN                     | 55 | AUSTRALIA              | 53 | JAPAN                         | 66 | ALBERTA, CANADA          | 58 | HUNGARY               | 59 |
| LATVIA                    | 50 | JAPAN                  | 52 | AUSTRALIA                     | 65 | ONTARIO, CANADA          | 58 | UNITED STATES         | 59 |
| NETHERLANDS               | 49 | ONTARIO, CANADA        | 52 | HONG KONG SAR                 | 65 | MINNESOTA, US            | 57 | SLOVENIA              | 58 |
| AUSTRALIA                 | 48 | ENGLAND                | 52 | CZECH REPUBLIC                | 65 | ENGLAND                  | 57 | CZECH REPUBLIC        | 58 |
| HUNGARY                   | 48 | UNITED STATES          | 52 | UNITED STATES                 | 65 | AUSTRIA                  | 55 | QUEBEC, CANADA        | 57 |
| SLOVENIA                  | 47 | SLOVENIA               | 51 | ONTARIO, CANADA               | 64 | UNITED STATES            | 55 | ALBERTA, CANADA       | 57 |
| CZECH REPUBLIC            | 47 | NETHERLANDS            | 50 | ENGLAND                       | 64 | AUSTRALIA                | 54 | ONTARIO, CANADA       | 56 |
| IRAN, ISLAMIC REP. OF     | 47 | HONG KONG SAR          | 49 | SLOVENIA                      | 64 | CZECH REPUBLIC           | 54 | AUSTRALIA             | 55 |
| International Average     | 45 | NEW ZEALAND            | 48 | QUEBEC, CANADA                | 62 | SLOVENIA                 | 53 | NETHERLANDS           | 52 |
| AUSTRIA                   | 44 | QUEBEC, CANADA         | 48 | NEW ZEALAND                   | 59 | NEW ZEALAND              | 53 | SCOTLAND              | 52 |
| SCOTLAND                  | 44 | SCOTLAND               | 44 | NORWAY                        | 57 | NORWAY                   | 51 | International Average | 50 |
| NEW ZEALAND               | 44 | International Average  | 43 | SCOTLAND                      | 57 | SCOTLAND                 | 49 | NEW ZEALAND           | 50 |
| QUEBEC, CANADA            | 43 | NORWAY                 | 42 | International Average         | 55 | International Average    | 48 | NORWAY                | 48 |
| NORWAY                    | 35 | IRAN, ISLAMIC REP. OF  | 34 | IRAN, ISLAMIC REP. OF         | 47 | IRAN, ISLAMIC REP. OF    | 40 | IRAN, ISLAMIC REP. OF | 38 |
| KUWAIT                    | 33 | KUWAIT                 | 20 | TUNISIA                       | 31 | TUNISIA                  | 25 | KUWAIT                | 31 |
| TUNISIA                   | 23 | TUNISIA                | 18 | KUWAIT                        | 29 | KUWAIT                   | 24 | TUNISIA               | 29 |

Figure 30



| Grade 4 Science Topics        |    |                             |    |                       |    |                                 |    |                       |    |
|-------------------------------|----|-----------------------------|----|-----------------------|----|---------------------------------|----|-----------------------|----|
| Energy and Physical Processes |    | Physical & Chemical Changes |    | Forces and Motion     |    | Environmental & Resource Issues |    | Scientific Processes  |    |
| SINGAPORE                     | 73 | SINGAPORE                   | 69 | HONG KONG SAR         | 71 | ALBERTA, CANADA                 | 67 | SINGAPORE             | 70 |
| JAPAN                         | 67 | JAPAN                       | 65 | SINGAPORE             | 70 | MINNESOTA, US                   | 63 | HONG KONG SAR         | 70 |
| HONG KONG SAR                 | 61 | HONG KONG SAR               | 61 | MINNESOTA, US         | 67 | QUEBEC, CANADA                  | 62 | ENGLAND               | 69 |
| MINNESOTA, US                 | 58 | LATVIA                      | 60 | ONTARIO, CANADA       | 64 | SINGAPORE                       | 62 | MINNESOTA, US         | 67 |
| LATVIA                        | 58 | HUNGARY                     | 58 | ALBERTA, CANADA       | 63 | HONG KONG SAR                   | 61 | LATVIA                | 67 |
| ENGLAND                       | 56 | MINNESOTA, US               | 57 | AUSTRIA               | 63 | ONTARIO, CANADA                 | 61 | UNITED STATES         | 67 |
| ALBERTA, CANADA               | 56 | ENGLAND                     | 57 | AUSTRALIA             | 62 | JAPAN                           | 59 | AUSTRALIA             | 67 |
| UNITED STATES                 | 55 | SLOVENIA                    | 56 | LATVIA                | 62 | AUSTRALIA                       | 58 | JAPAN                 | 65 |
| ONTARIO, CANADA               | 54 | CZECH REPUBLIC              | 55 | ENGLAND               | 62 | ITALY                           | 58 | ALBERTA, CANADA       | 64 |
| HUNGARY                       | 54 | ITALY                       | 55 | UNITED STATES         | 61 | ENGLAND                         | 58 | NETHERLANDS           | 63 |
| NETHERLANDS                   | 54 | ALBERTA, CANADA             | 55 | JAPAN                 | 61 | UNITED STATES                   | 57 | HUNGARY               | 62 |
| SLOVENIA                      | 54 | UNITED STATES               | 55 | ITALY                 | 61 | NETHERLANDS                     | 57 | ITALY                 | 61 |
| ITALY                         | 53 | ONTARIO, CANADA             | 53 | NETHERLANDS           | 60 | HUNGARY                         | 57 | QUEBEC, CANADA        | 61 |
| AUSTRIA                       | 53 | AUSTRIA                     | 51 | NEW ZEALAND           | 60 | AUSTRIA                         | 55 | ONTARIO, CANADA       | 61 |
| AUSTRALIA                     | 53 | AUSTRALIA                   | 51 | HUNGARY               | 58 | LATVIA                          | 55 | SCOTLAND              | 61 |
| CZECH REPUBLIC                | 50 | QUEBEC, CANADA              | 50 | SCOTLAND              | 56 | SCOTLAND                        | 52 | NEW ZEALAND           | 60 |
| NEW ZEALAND                   | 49 | NETHERLANDS                 | 49 | International Average | 54 | SLOVENIA                        | 52 | AUSTRIA               | 60 |
| QUEBEC, CANADA                | 48 | International Average       | 46 | SLOVENIA              | 54 | CZECH REPUBLIC                  | 51 | SLOVENIA              | 58 |
| SCOTLAND                      | 48 | NEW ZEALAND                 | 45 | CZECH REPUBLIC        | 54 | NEW ZEALAND                     | 51 | CZECH REPUBLIC        | 57 |
| International Average         | 47 | SCOTLAND                    | 44 | NORWAY                | 53 | International Average           | 45 | International Average | 56 |
| NORWAY                        | 42 | NORWAY                      | 40 | QUEBEC, CANADA        | 52 | IRAN, ISLAMIC REP. OF           | 42 | NORWAY                | 54 |
| IRAN, ISLAMIC REP. OF         | 38 | IRAN, ISLAMIC REP. OF       | 35 | IRAN, ISLAMIC REP. OF | 45 | NORWAY                          | 41 | IRAN, ISLAMIC REP. OF | 45 |
| TUNISIA                       | 28 | KUWAIT                      | 26 | KUWAIT                | 42 | KUWAIT                          | 22 | KUWAIT                | 37 |
| KUWAIT                        | 26 | TUNISIA                     | 25 | TUNISIA               | 39 | TUNISIA                         | 19 | TUNISIA               | 35 |

|                                     |
|-------------------------------------|
| Significantly higher than MN        |
| Not Statistically Different from MN |
| Significantly lower than MN         |

Figure 31

## Grade 8 Science

- Minnesota students scored significantly lower than students in five countries: China, Korea, Singapore, Hong Kong and Japan.
- Minnesota students scored significantly better than students from the other 44 participating countries.
- On specific categories of science, Minnesota students scored significantly lower than students in six other countries.
- Singapore and Japan scored higher on eight of the broad science categories displayed.
- Rep. of Korea scored higher on six of the broad science categories displayed.
- The Czech Republic scored higher on five of the broad science categories-Properties and Classification of Matter; Structure of Matter; Energy and Physical Processes; Physical Changes; and Forces and Motion.
- Hungary scored higher on four of the broad science categories- Properties and Classification of Matter; Structure of Matter; Energy and Physical Processes; and Physical Changes.
- The Russian Federation Scored higher on three of the broad science categories-Properties and Classification of Matter; Structure of Matter; and Physical Changes.
- Hong Kong scored higher on two of the broad science categories-Life Cycles and Genetics and Energy and Physical Processes.
- MN students scored significantly higher than the U.S. students in seven areas of science-Earth Features and Processes; Diversity and Structure of Living Things; Interaction of Living Things; Human Biology and Health; Environmental and Resource Issues and Scientific Processes.
- Although MN students scored higher than the US students in all but one of the other broad categories, the differences were not statistically significant.

(Figures 32 and 33)

Display 4: Grade 8 Science Topics

| Earth Features                | Earth Processes          | Earth in the Universe                 | Diversity & Structure of Living Things | Life Processes & Functions    | Life Cycles & Genetics   |
|-------------------------------|--------------------------|---------------------------------------|--|-------------------------------|--------------------------|
| MINNESOTA, US 61              | CZECH REPUBLIC 60        | SLOVENIA 63                           | SINGAPORE 61                           | SINGAPORE 68                  | KOREA, REP. OF 65        |
| SLOVENIA 60                   | HONG KONG SAR 60         | CZECH REPUBLIC 61                     | KOREA, REP. OF 60                      | KOREA, REP. OF 63             | JAPAN 60                 |
| HUNGARY 59                    | JAPAN 59                 | KOREA, REP. OF 60                     | MINNESOTA, US 68                       | JAPAN 62                      | HONG KONG SAR 60         |
| CZECH REPUBLIC 59             | MINNESOTA, US 68         | MINNESOTA, US 60                      | JAPAN 57                               | HONG KONG SAR 59              | SINGAPORE 57             |
| JAPAN 58                      | SLOVENIA 58              | UNITED STATES 68                      | HUNGARY 56                             | ENGLAND 58                    | RUSSIAN FEDERATION 52    |
| RUSSIAN FEDERATION 57         | RUSSIAN FEDERATION 57    | SWEDEN 57                             | CZECH REPUBLIC 56                      | MINNESOTA, US 68              | HUNGARY 51               |
| KOREA, REP. OF 57             | ONTARIO, CANADA 56       | NORWAY 57                             | ONTARIO, CANADA 55                     | SLOVENIA 52                   | QUEBEC, CANADA 49        |
| SWEDEN 56                     | SINGAPORE 56             | SINGAPORE 57                          | SLOVENIA 55                            | RUSSIAN FEDERATION 52         | MINNESOTA, US 48         |
| NORWAY 54                     | QUEBEC, CANADA 53        | ENGLAND 56                            | LITHUANIA 55                           | UNITED STATES 62              | LITHUANIA 49             |
| ONTARIO, CANADA 53            | UNITED STATES 63         | RUSSIAN FEDERATION 55                 | ENGLAND 55                             | ONTARIO, CANADA 51            | UNITED STATES 47         |
| SINGAPORE 53                  | LITHUANIA 53             | BULGARIA 55                           | UNITED STATES 64                       | LITHUANIA 50                  | ENGLAND 47               |
| LITHUANIA 52                  | AUSTRALIA 52             | ITALY 55                              | RUSSIAN FEDERATION 53                  | CZECH REPUBLIC 47             | CZECH REPUBLIC 46        |
| UNITED STATES 61              | ENGLAND 52               | LITHUANIA 55                          | HONG KONG SAR 51                       | SWEDEN 47                     | AUSTRALIA 44             |
| AUSTRALIA 51                  | ITALY 51                 | AUSTRALIA 53                          | AUSTRALIA 50                           | AUSTRALIA 47                  | SLOVENIA 43              |
| ITALY 50                      | SWEDEN 51                | HONG KONG SAR 51                      | SWEDEN 48                              | SCOTLAND 47                   | BULGARIA 43              |
| HONG KONG SAR 50              | KOREA, REP. OF 50        | QUEBEC, CANADA 50                     | QUEBEC, CANADA 48                      | ITALY 45                      | ITALY 42                 |
| ENGLAND 50                    | HUNGARY 50               | ONTARIO, CANADA 50                    | ITALY 47                               | QUEBEC, CANADA 44             | SWEDEN 41                |
| QUEBEC, CANADA 49             | NORWAY 47                | HUNGARY 49                            | THAILAND 44                            | HUNGARY 43                    | ONTARIO, CANADA 41       |
| SCOTLAND 46                   | THAILAND 46              | THAILAND 49                           | SCOTLAND 43                            | International 43              | ISRAEL 39                |
| BULGARIA 45                   | SCOTLAND 46              | IRAN, ISLAMIC REP. OF 48              | BULGARIA 43                            | THAILAND 41                   | International 38         |
| ROMANIA 41                    | IRAN, ISLAMIC REP. OF 45 | JAPAN 48                              | NORWAY 42                              | BULGARIA 40                   | NORWAY 38                |
| International 38              | BULGARIA 44              | SCOTLAND 46                           | International 41                       | ROMANIA 38                    | SCOTLAND 37              |
| ISRAEL 37                     | International 41         | International 45                      | ISRAEL 41                              | NORWAY 38                     | THAILAND 35              |
| IRAN, ISLAMIC REP. OF 35      | ISRAEL 40                | ROMANIA 39                            | ROMANIA 38                             | ISRAEL 38                     | IRAN, ISLAMIC REP. OF 34 |
| THAILAND 34                   | ROMANIA 39               | ISRAEL 38                             | IRAN, ISLAMIC REP. OF 36               | KUWAIT 38                     | CYPRUS 34                |
| CYPRUS 31                     | CYPRUS 38                | KUWAIT 35                             | CYPRUS 34                              | CYPRUS 36                     | COLOMBIA 33              |
| COLOMBIA 28                   | COLOMBIA 29              | CYPRUS 35                             | COLOMBIA 34                            | COLOMBIA 34                   | KUWAIT 30                |
| KUWAIT 16                     | KUWAIT 27                | COLOMBIA 34                           | KUWAIT 32                              | IRAN, ISLAMIC REP. OF 31      | ROMANIA 29               |
| Interactions of Living Things | Human Biology and Health | Properties & Classification of Matter | Structure of Matter                    | Energy and Physical Processes | Physical Changes         |
| SINGAPORE 64                  | MINNESOTA, US 70         | SINGAPORE 53                          | SLOVENIA 66                            | SINGAPORE 63                  | KOREA, REP. OF 57        |
| KOREA, REP. OF 62             | KOREA, REP. OF 69        | KOREA, REP. OF 53                     | SINGAPORE 64                           | KOREA, REP. OF 59             | SINGAPORE 55             |
| MINNESOTA, US 62              | CZECH REPUBLIC 66        | SLOVENIA 51                           | CZECH REPUBLIC 60                      | JAPAN 58                      | JAPAN 53                 |
| HUNGARY 60                    | ENGLAND 66               | JAPAN 50                              | RUSSIAN FEDERATION 60                  | ENGLAND 54                    | ENGLAND 52               |
| SLOVENIA 60                   | HUNGARY 65               | HUNGARY 50                            | HUNGARY 57                             | HUNGARY 54                    | RUSSIAN FEDERATION 49    |
| JAPAN 59                      | JAPAN 65                 | CZECH REPUBLIC 49                     | LITHUANIA 54                           | CZECH REPUBLIC 52             | SLOVENIA 49              |
| ENGLAND 58                    | ONTARIO, CANADA 64       | RUSSIAN FEDERATION 48                 | BULGARIA 53                            | HONG KONG SAR 51              | HUNGARY 49               |
| ONTARIO, CANADA 58            | SINGAPORE 64             | ENGLAND 47                            | JAPAN 52                               | RUSSIAN FEDERATION 49         | CZECH REPUBLIC 47        |
| LITHUANIA 58                  | QUEBEC, CANADA 64        | HONG KONG SAR 44                      | ROMANIA 50                             | SLOVENIA 47                   | LITHUANIA 45             |
| CZECH REPUBLIC 57             | SWEDEN 63                | MINNESOTA, US 41                      | IRAN, ISLAMIC REP. OF 49               | ONTARIO, CANADA 46            | HONG KONG SAR 45         |
| UNITED STATES 67              | UNITED STATES 68         | LITHUANIA 40                          | UNITED STATES 48                       | SWEDEN 45                     | SWEDEN 44                |
| HONG KONG SAR 55              | HONG KONG SAR 63         | SWEDEN 40                             | CYPRUS 47                              | AUSTRALIA 45                  | ONTARIO, CANADA 44       |
| AUSTRALIA 55                  | RUSSIAN FEDERATION 62    | UNITED STATES 40                      | MINNESOTA, US 48                       | MINNESOTA, US 46              | MINNESOTA, US 43         |
| RUSSIAN FEDERATION 55         | AUSTRALIA 62             | AUSTRALIA 39                          | ITALY 44                               | LITHUANIA 44                  | AUSTRALIA 42             |
| SWEDEN 53                     | ITALY 61                 | ONTARIO, CANADA 39                    | ISRAEL 44                              | SCOTLAND 44                   | UNITED STATES 41         |
| QUEBEC, CANADA 52             | NORWAY 59                | QUEBEC, CANADA 38                     | SWEDEN 44                              | UNITED STATES 43              | NORWAY 40                |
| SCOTLAND 48                   | SLOVENIA 58              | SCOTLAND 37                           | International 43                       | ITALY 43                      | QUEBEC, CANADA 40        |
| NORWAY 46                     | THAILAND 57              | ISRAEL 37                             | ENGLAND 42                             | QUEBEC, CANADA 42             | SCOTLAND 40              |
| ITALY 46                      | LITHUANIA 56             | BULGARIA 36                           | KOREA, REP. OF 42                      | BULGARIA 41                   | ISRAEL 39                |
| ISRAEL 44                     | SCOTLAND 54              | International 35                      | QUEBEC, CANADA 37                      | International 40              | CYPRUS 39                |
| THAILAND 43                   | ISRAEL 54                | ITALY 34                              | KUWAIT 37                              | ROMANIA 39                    | ITALY 38                 |
| International 42              | ROMANIA 52               | NORWAY 34                             | AUSTRALIA 35                           | IRAN, ISLAMIC REP. OF 39      | BULGARIA 37              |
| ROMANIA 41                    | BULGARIA 51              | CYPRUS 34                             | THAILAND 35                            | NORWAY 39                     | International 37         |
| BULGARIA 40                   | International 50         | THAILAND 33                           | COLOMBIA 33                            | CYPRUS 38                     | IRAN, ISLAMIC REP. OF 36 |
| IRAN, ISLAMIC REP. OF 38      | CYPRUS 49                | ROMANIA 33                            | NORWAY 31                              | ISRAEL 38                     | ROMANIA 34               |
| CYPRUS 37                     | IRAN, ISLAMIC REP. OF 48 | IRAN, ISLAMIC REP. OF 32              | SCOTLAND 30                            | THAILAND 38                   | THAILAND 34              |
| COLOMBIA 31                   | COLOMBIA 43              | KUWAIT 27                             | HONG KONG SAR 29                       | KUWAIT 36                     | KUWAIT 28                |
| KUWAIT 28                     | KUWAIT 38                | COLOMBIA 24                           | ONTARIO, CANADA 29                     | COLOMBIA 30                   | COLOMBIA 25              |

Figure 32



Display 4: Grade 8 Science Topics

| Chemical Changes      |    | Force and Motion      |    | Science, Technology, & Society |    | Environmental & Resource Issues |    | Scientific Processes  |    |
|-----------------------|----|-----------------------|----|--------------------------------|----|---------------------------------|----|-----------------------|----|
| ENGLAND               | 55 | CZECH REPUBLIC        | 49 | SINGAPORE                      | 51 | SINGAPORE                       | 55 | JAPAN                 | 56 |
| SINGAPORE             | 55 | JAPAN                 | 49 | JAPAN                          | 50 | MINNESOTA, US                   | 66 | SINGAPORE             | 52 |
| HONG KONG SAR         | 48 | KOREA, REP. OF        | 48 | QUEBEC, CANADA                 | 44 | SLOVENIA                        | 53 | KOREA, REP. OF        | 50 |
| JAPAN                 | 47 | SINGAPORE             | 48 | CZECH REPUBLIC                 | 44 | ONTARIO, CANADA                 | 53 | MINNESOTA, US         | 48 |
| SLOVENIA              | 45 | ENGLAND               | 45 | RUSSIAN FEDERATION             | 44 | ENGLAND                         | 53 | ENGLAND               | 46 |
| AUSTRALIA             | 45 | SLOVENIA              | 44 | ENGLAND                        | 41 | AUSTRALIA                       | 52 | ONTARIO, CANADA       | 45 |
| MINNESOTA, US         | 46 | HUNGARY               | 44 | ONTARIO, CANADA                | 40 | HUNGARY                         | 51 | CZECH REPUBLIC        | 45 |
| SCOTLAND              | 44 | ONTARIO, CANADA       | 43 | HONG KONG SAR                  | 39 | KOREA, REP. OF                  | 51 | HONG KONG SAR         | 43 |
| RUSSIAN FEDERATION    | 44 | MINNESOTA, US         | 43 | KOREA, REP. OF                 | 39 | HONG KONG SAR                   | 50 | UNITED STATES         | 43 |
| HUNGARY               | 43 | LITHUANIA             | 42 | MINNESOTA, US                  | 38 | LITHUANIA                       | 50 | SLOVENIA              | 42 |
| UNITED STATES         | 43 | HONG KONG SAR         | 42 | UNITED STATES                  | 37 | RUSSIAN FEDERATION              | 49 | AUSTRALIA             | 42 |
| ONTARIO, CANADA       | 43 | RUSSIAN FEDERATION    | 41 | ITALY                          | 36 | UNITED STATES                   | 48 | QUEBEC, CANADA        | 40 |
| LITHUANIA             | 40 | SWEDEN                | 41 | AUSTRALIA                      | 36 | CZECH REPUBLIC                  | 48 | HUNGARY               | 40 |
| CZECH REPUBLIC        | 39 | UNITED STATES         | 40 | HUNGARY                        | 34 | QUEBEC, CANADA                  | 48 | LITHUANIA             | 40 |
| IRAN, ISLAMIC REP. OF | 38 | AUSTRALIA             | 38 | SCOTLAND                       | 33 | JAPAN                           | 48 | RUSSIAN FEDERATION    | 38 |
| BULGARIA              | 38 | QUEBEC, CANADA        | 36 | CYPRUS                         | 32 | SCOTLAND                        | 46 | SCOTLAND              | 36 |
| QUEBEC, CANADA        | 38 | SCOTLAND              | 33 | SLOVENIA                       | 31 | SWEDEN                          | 43 | ISRAEL                | 34 |
| KOREA, REP. OF        | 37 | ITALY                 | 33 | IRAN, ISLAMIC REP. OF          | 28 | ITALY                           | 43 | SWEDEN                | 34 |
| NORWAY                | 35 | NORWAY                | 32 | SWEDEN                         | 26 | NORWAY                          | 42 | ITALY                 | 30 |
| International         | 34 | ISRAEL                | 32 | BULGARIA                       | 26 | THAILAND                        | 40 | THAILAND              | 29 |
| SWEDEN                | 34 | International         | 31 | International                  | 26 | ROMANIA                         | 39 | International         | 29 |
| ITALY                 | 32 | THAILAND              | 29 | LITHUANIA                      | 25 | CYPRUS                          | 38 | NORWAY                | 28 |
| ROMANIA               | 31 | BULGARIA              | 29 | ROMANIA                        | 24 | International                   | 38 | CYPRUS                | 25 |
| THAILAND              | 31 | ROMANIA               | 28 | COLOMBIA                       | 23 | BULGARIA                        | 36 | ROMANIA               | 25 |
| ISRAEL                | 30 | IRAN, ISLAMIC REP. OF | 27 | THAILAND                       | 19 | ISRAEL                          | 35 | BULGARIA              | 24 |
| KUWAIT                | 27 | KUWAIT                | 23 | KUWAIT                         | 19 | IRAN, ISLAMIC REP. OF           | 35 | IRAN, ISLAMIC REP. OF | 22 |
| CYPRUS                | 24 | COLOMBIA              | 18 | NORWAY                         | 17 | COLOMBIA                        | 28 | KUWAIT                | 19 |
| COLOMBIA              | 22 | CYPRUS                | 16 | ISRAEL                         | 16 | KUWAIT                          | 21 | COLOMBIA              | 15 |

|                                     |
|-------------------------------------|
| Significantly higher than MN        |
| Not Statistically Different from MN |
| Significantly lower than MN         |

Figure 33

## TEACHING TIME ON SCIENCE TOPICS: A COMPARISON OF 1995 AND 2007 MN DATA

### Grade 4 Science

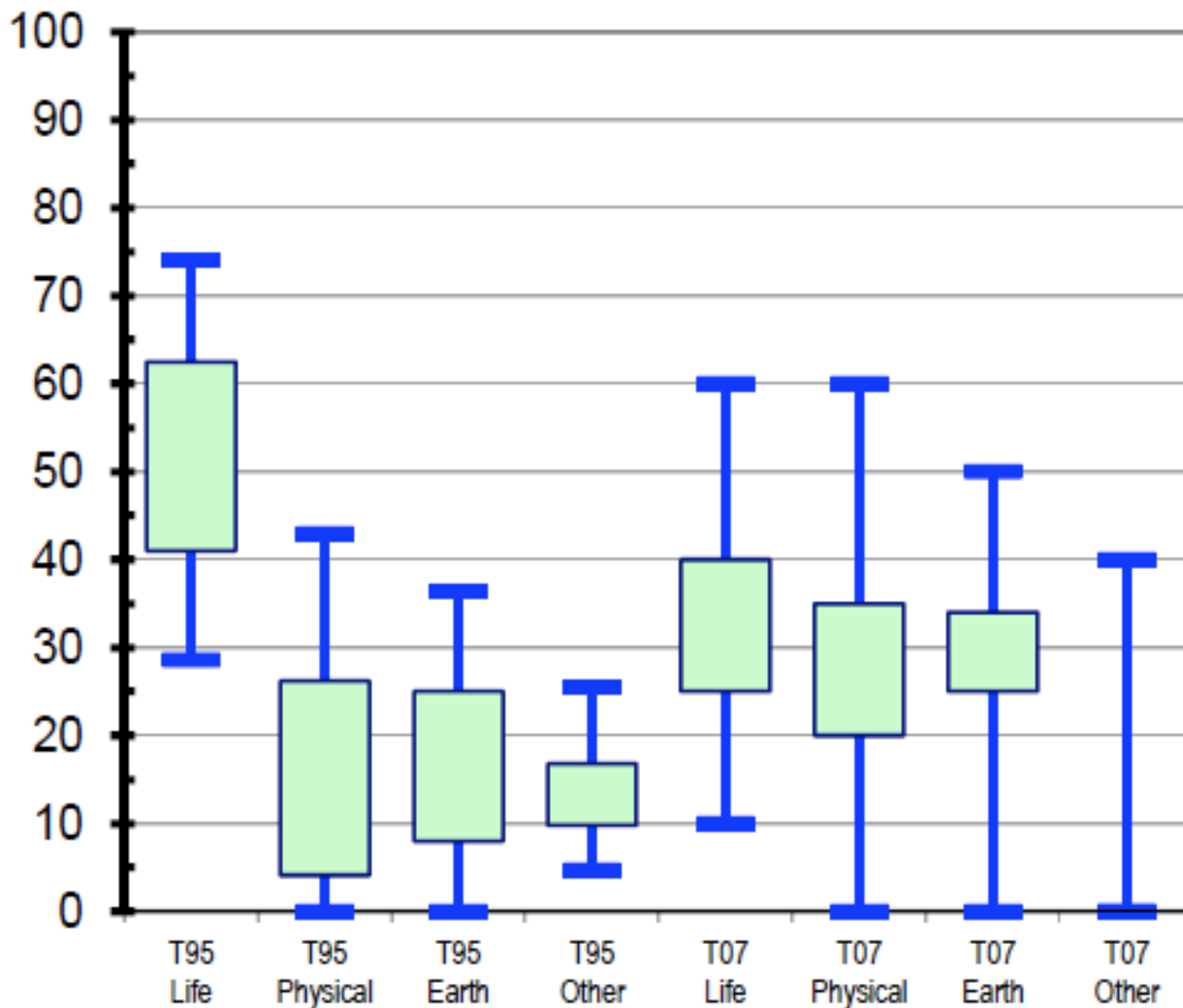


Figure 34

### GRADE 4

- Compared to 1995 when the reported median percent time on Life Science topics was about 50%, the median percent time on these topics decreased in 2007 to about 35%. However, the range in reported time in on these topics in 2007 appears to have widened. (Figure 34)
- The typical percentage of reported time teachers spent on Physical and Earth Science topics show an increase compared to the 1995 data. The increase in typical reported time is coupled with an increase in the variability in time spent on these topics.



## Grade 8 Science

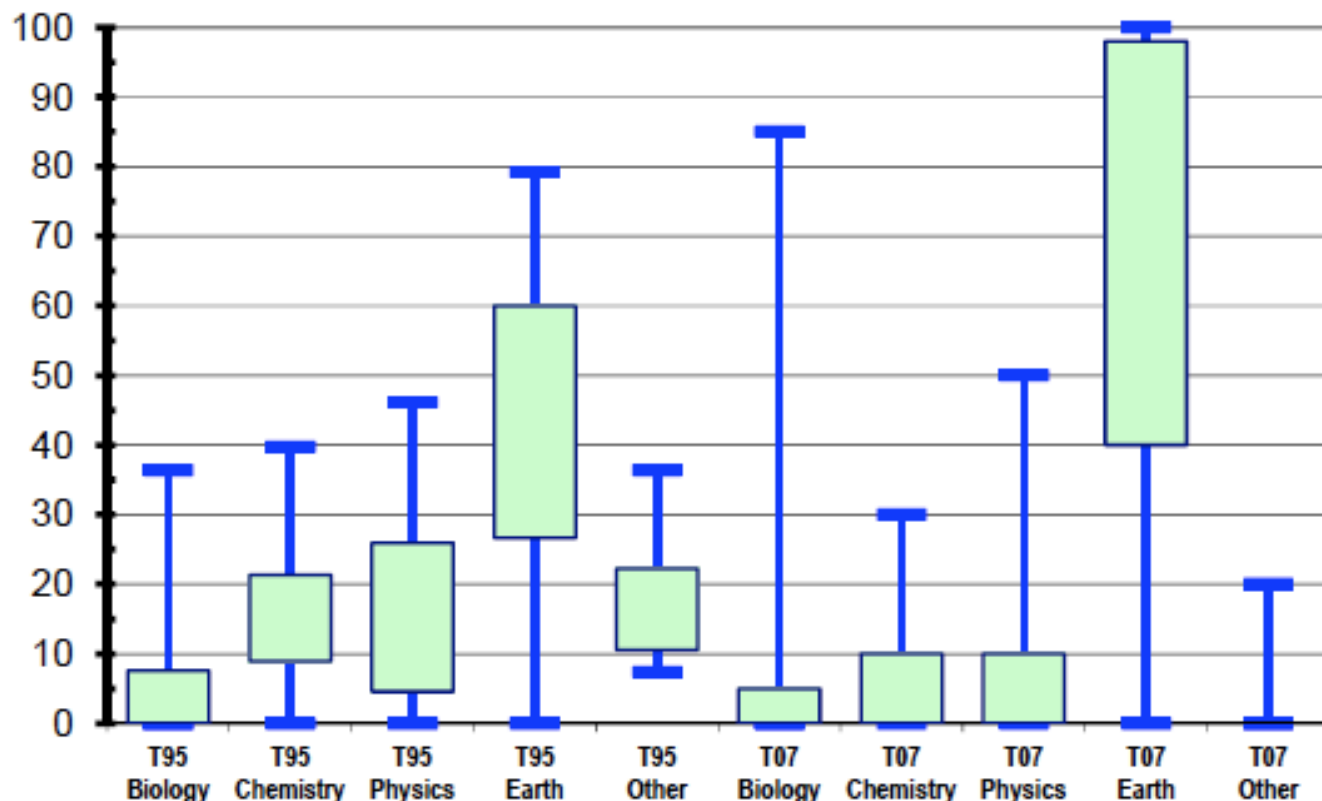


Figure 35

### Grade 8 Science (Figure 35)

- The median percentage of time reported on Earth Science topics in 2007 was approximately 70% compared to about 45% in 1995.
- The increase in typical percent time on Earth Science in 2007 is coupled with increased variability. In at least one classroom teacher reports indicate that no time is devoted to Earth Science. In contrast, there is at least another MN classroom where 100% of teaching time is devoted to Earth Science.
- Compared to 1995, teachers in 2007 report spending less time (on average) on Chemistry, Physics and “other” science topics.
- Although three-quarters of the reported percent time spent on teaching Biology topics in 2007 is less than 5%, there is at least one classroom where the reported percent time on Biology topics is about 85%.

## MN SCIENCE CURRICULUM: COMPARISON TO TOP ACHIEVING COUNTRIES

- Intended topic coverage appears scattered and not coherent compared to the composite of the majority of top achieving countries. The curriculum lacked the structure that is required to allow for the development of concepts as they relate to science themes.
- Too many topics were intended to be covered in the early grades. Too few are intended for coverage in the middle school grades. With the abundance of topics intended for coverage in grades one through four, there is little opportunity to develop any deep understanding of science content.
- Some topics were intended for coverage too early, before their time, and then dropped from coverage, and therefore not developed fully throughout the middle grades. Examples are: Atoms, Ions, and Molecules; Chemical Changes of Matter; Sound & Vibration; and Magnetism. Content related to these topics should be included in the curriculum during the middle grades so that students can establish a foundation of knowledge that will enable them to grasp more complex ideas related to

chemistry and physics when they reach high school.

- All courses specific to a discipline – earth, life, or physical science – carry a high concentration of content areas in their discipline. This is expected but coverage of physical science topics appears to be particularly weak. Physical science topics intended in only one grade or never intended include: Classification of Matter; Atoms, Ions, and Molecules; Chemical Properties of Matter; Chemical Changes of Matter; and Explanations of Physical Changes.
- Other topics from other disciplines were not specifically intended for coverage in any of the eight grades. They include: Earth's Composition; Land, Water, Sea Resource Conservation; Material & Energy Resource Conservation; Pollution; and Human Nutrition.
- On a positive note, one topic, Energy Types, Sources, Conversions, was intended in four consecutive grades. This likely allows for very thorough development of content related to this topic.

(Figure 36)

## Science Topics Intended at Each Grade in the state of Minnesota

| Topics                                  | Grade |   |   |   |   |   |   |   |
|---|-------|---|---|---|---|---|---|---|
|   | 1     | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| Organs, Tissues                         | ●     |   | ● | ● |   |   | ● |   |
| Physical Properties of Matter           | ●     | ● |   | ● |   | ● |   | ● |
| Plants, Fungi                           | ●     | ● | ● | ● |   |   | ● |   |
| Animals                                 | ●     | ● | ● | ● |   |   | ● |   |
| Classification of Matter                |       |   |   |   |   | ● |   |   |
| Rocks, Soil                             |       | ● |   |   | ● |   |   | ● |
| Light                                   |       |   | ● |   |   | ● |   |   |
| Electricity                             |       |   |   | ● |   | ● |   |   |
| Life Cycles                             | ●     | ● |   |   | ● |   |   |   |
| Physical Changes of Matter              |       | ● |   | ● |   | ● |   |   |
| Heat & Temperature                      |       |   |   | ● |   | ● |   | ● |
| Bodies of Water                         |       | ● |   | ● | ● |   |   | ● |
| Interdependence of Life                 | ●     | ● | ● |   | ● |   | ● | ● |
| Habitats & Niches                       |       |   | ● |   |   |   |   |   |
| Biomes & Ecosystems                     |       |   |   |   | ● |   | ● |   |
| Reproduction                            |       |   | ● |   |   |   | ● |   |
| Time, Space, Motion                     |       | ● |   |   |   | ● |   |   |
| Types of Forces                         | ●     |   |   | ● |   | ● |   | ● |
| Weather & Climate                       | ●     |   |   |   |   |   |   | ● |
| Planets in the Solar System             |       |   | ● |   |   |   |   | ● |
| Magnetism                               | ●     | ● |   | ● |   | ● |   |   |
| Earth's Composition                     |       |   |   |   |   |   |   |   |
| Organism Energy Handling                |       |   |   |   | ● |   | ● |   |
| Land, Water, Sea Resource Conservation  |       |   |   |   |   |   |   |   |
| Earth in the Solar System               | ●     |   | ● | ● | ● |   |   | ● |
| Atoms, Ions, Molecules                  |       |   |   |   |   | ● |   |   |
| Chemical Properties of Matter           |       |   |   |   |   |   |   |   |
| Chemical Changes of Matter              |       |   |   |   |   | ● |   |   |
| Physical Cycles                         |       |   |   | ● | ● |   |   | ● |
| Land Forms                              |       |   |   |   | ● |   |   |   |
| Material & Energy Resource Conservation |       |   |   |   |   |   |   |   |
| Explanations of Physical Changes        |       |   |   |   |   |   |   |   |
| Pollution                               |       |   |   |   |   |   |   |   |
| Atmosphere                              |       | ● |   |   | ● |   |   | ● |
| Sound & Vibration                       |       |   | ● |   |   | ● |   |   |
| Cells                                   |       |   |   | ● |   |   | ● |   |
| Human Nutrition                         |       |   |   |   |   |   |   |   |
| Building & Breaking                     |       |   |   |   | ● |   |   | ● |
| Energy Types, Sources, Conversions      |       |   |   |   | ● | ● | ● | ● |
| Dynamics of Motion                      |       | ● |   |   | ● | ● |   |   |
| Organism Sensing & Responding           |       |   |   |   |   |   | ● |   |

Figure 36

## NUMBER OF SCIENCE TOPICS INTENDED IN MINNESOTA SCHOOLS BY GRADE LEVEL (OUT OF 41 TOPICS)

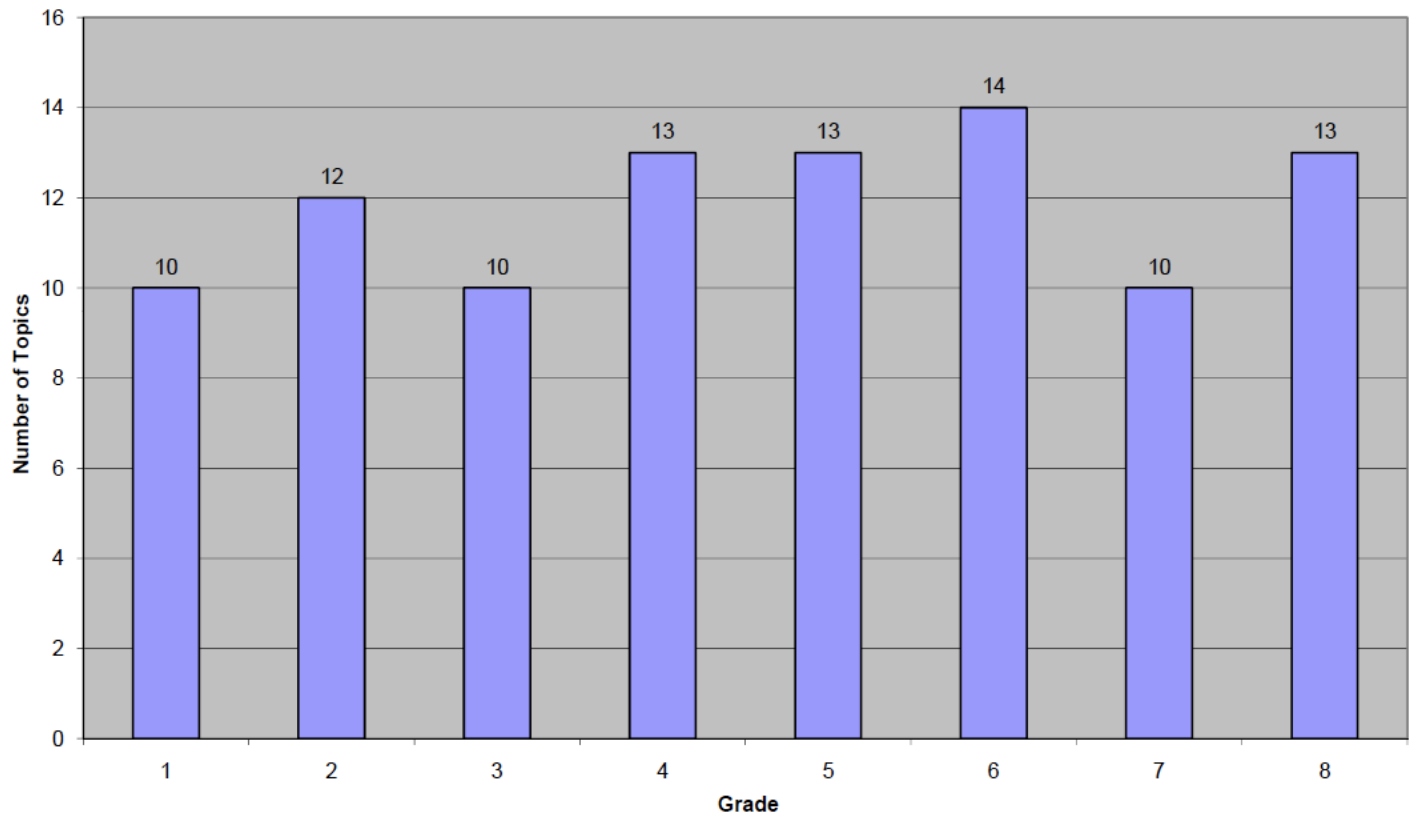


Figure 37

The above analysis is based upon implementation of the 2005 MN science standards. Those standards were revised in 2009 to address a number of concerns, including a number mentioned above. (Figure 37)

Figure 38 shows the comparison between 1995 and 2007 in time spent on the most important topics at

grade 4 in science. Notice how the amount of time spent on “other” (non-important) topics is reduced in 2007. Figure 39 shows how the 2007 time spent compares to the international focus and TIMSS test.

Figures 40 and 41 show the same information for grade 8 science.

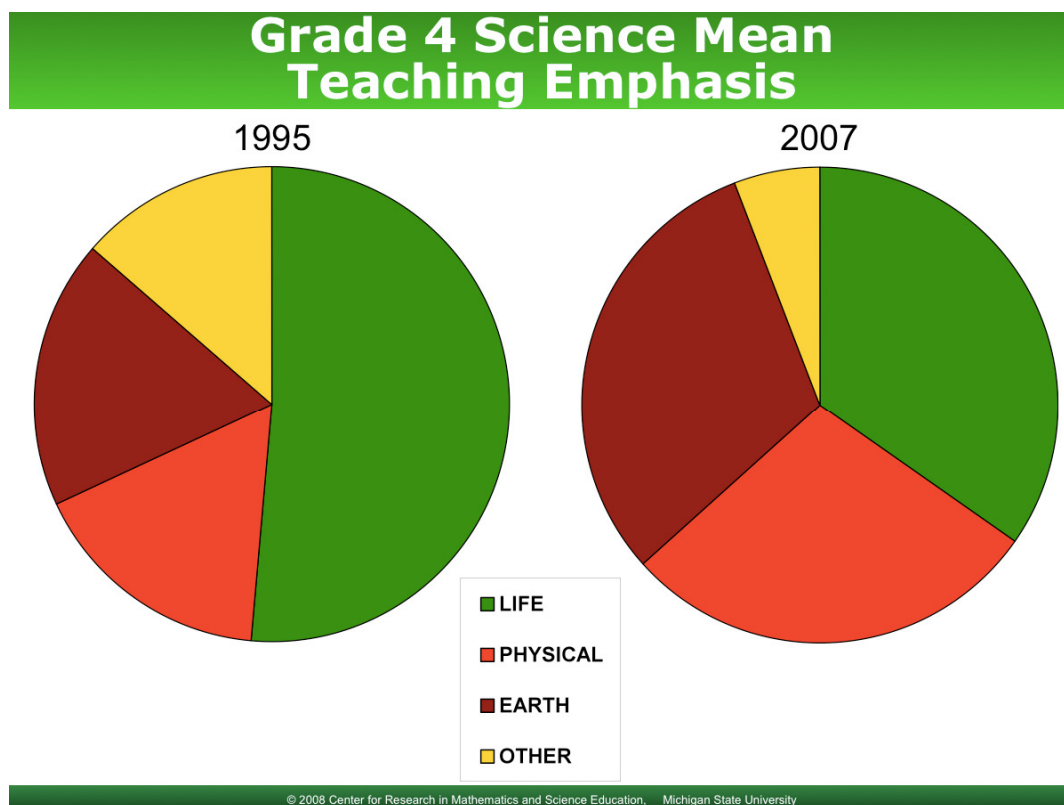


Figure 38

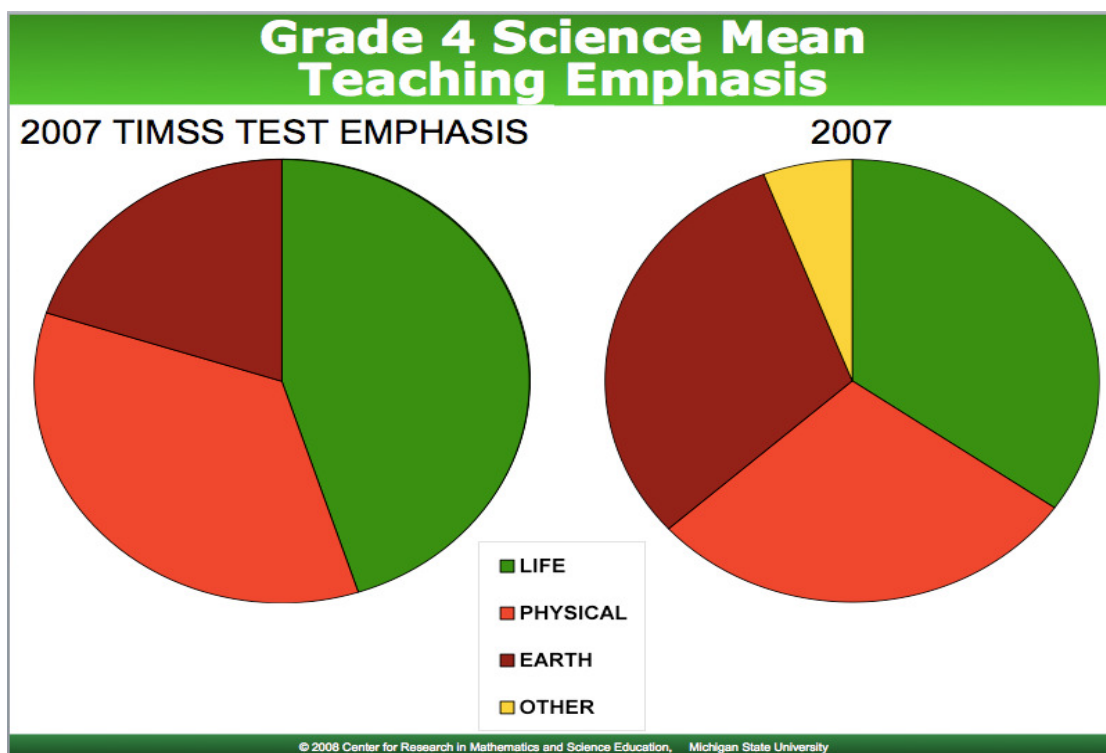


Figure 39

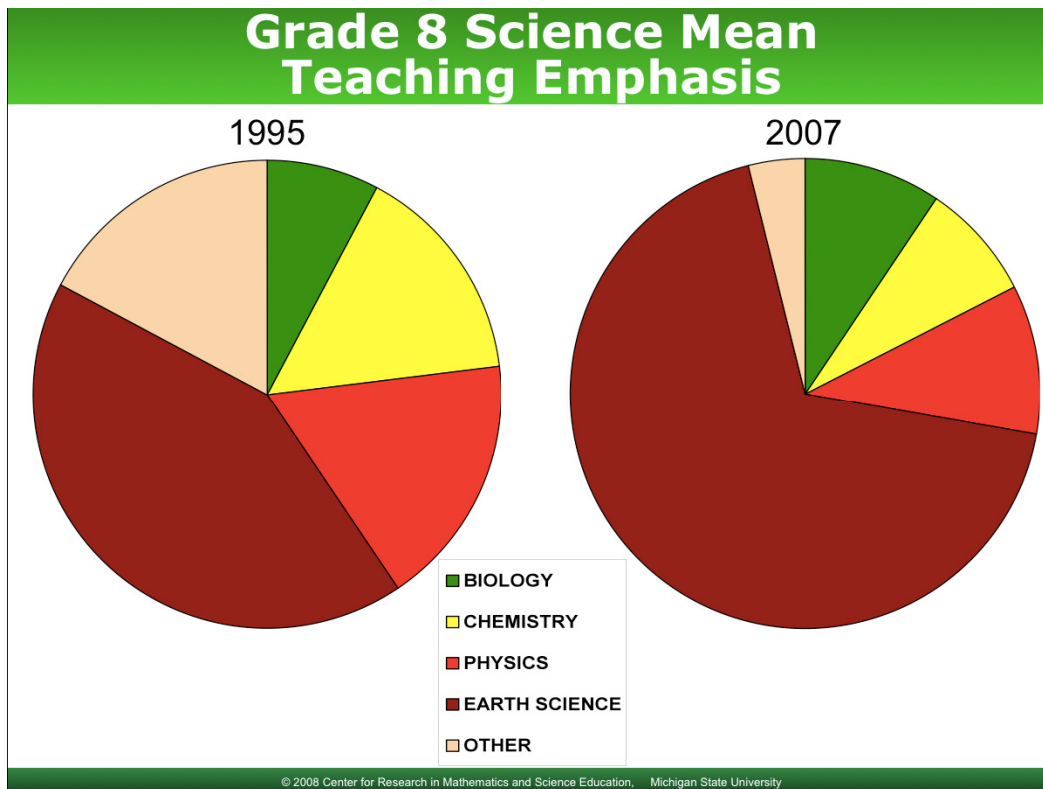


Figure 40

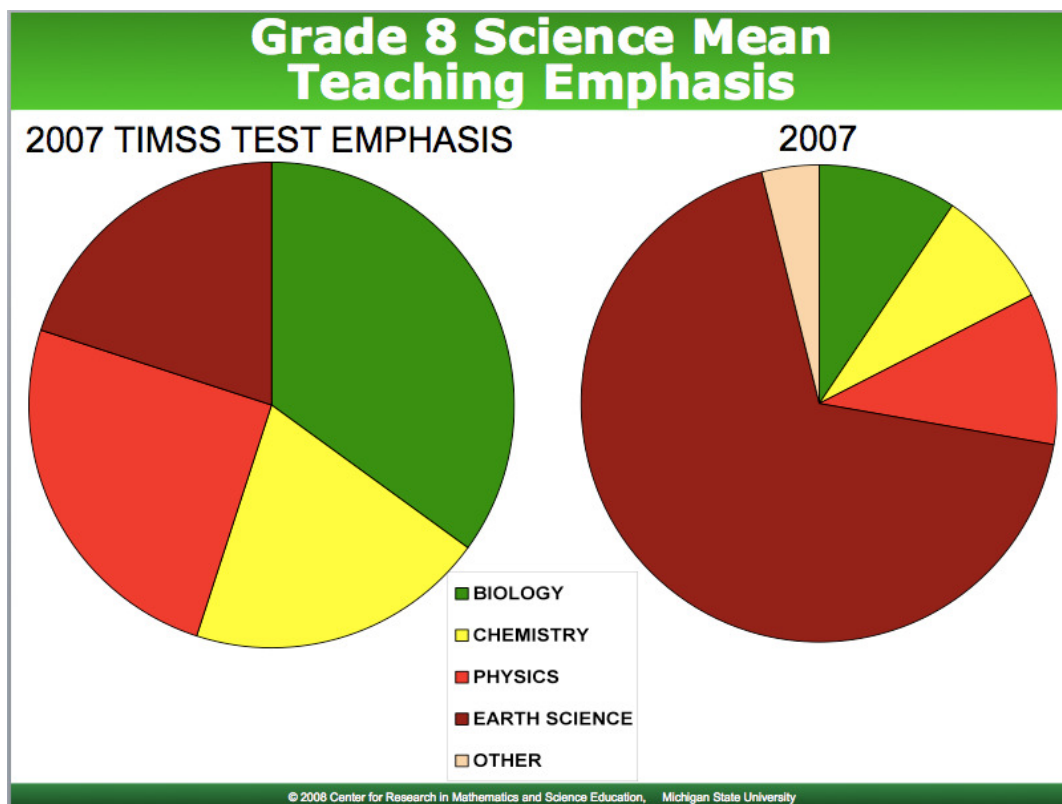


Figure 41

## CONCLUSIONS: WHAT CAN MINNESOTA LEARN FROM TIMSS 1995 AND 2007?

Minnesota has made great progress since 1995; it appears that internationally benchmarking our standards has brought significant benefit to our state in achieving a focused, rigorous and coherent set of standards.

For MN students, the competition for jobs will not be just the surrounding states - rather our students will compete for jobs globally and must be prepared to compete successfully at that level. Those nations are not standing still - and neither can Minnesota. We must seek to continually improve our standards and our success in delivering that information to all students.

The TIMSS substrand information provides excellent insight into which particular topics in math or science need greater emphasis in the curriculum. This may be best accomplished through development of Standards Frameworks and quality statewide staff development.

As the national efforts for Common Core Standards evolve, it may be possible to achieve efficiencies in resource development by collaborating with Massachusetts and other states.

It is clear that some Minnesota students are being left behind - particularly student subgroups that are in poverty. Though solutions to this problem have been elusive, the TIMSS analysis brings to light the fact that students in poverty are often not exposed to the correct level of rigorous content, therefore they might not even have the opportunity to learn that content.

Further analysis will bring additional insights into next steps for Minnesota educators and policymakers, especially in the area of Science. Check the SciMathMN website for updates to this TIMSS report. ([www.scimathmn.org](http://www.scimathmn.org))



## FOR FURTHER INFORMATION ABOUT TIMSS...

For U.S. TIMSS Information:

- NCES U.S. TIMSS Website  
<http://www.ed.gov/NCES/timss>
- Boston College TIMSS Website  
<http://timss.bc.edu/>
- Michigan State University U.S. 1995 TIMSS Website  
<http://ustimss.msu.edu>

For Minnesota TIMSS Information:

- Call SciMath<sup>MN</sup> at 612-209-1739
- E-mail [info@scimathmn.org](mailto:info@scimathmn.org)
- Visit the SciMath<sup>MN</sup> website at  
[www.scimathmn.org](http://www.scimathmn.org)
- Summer 2008: Release of complete Minnesota TIMSS Report (expanded version of this preliminary summary) by SciMath<sup>MN</sup>.

- This document as well as the preliminary report will be posted on the SciMath<sup>MN</sup> website and may be downloaded in full color to enhance the interpretation of graphs.



## ABOUT SCIMATH<sup>MN</sup>...

Founded in 1993, SciMath<sup>MN</sup> is a partnership among business, education and state government pursuing statewide improvement in the teaching and learning of K-12 mathematics, science and technology education based on the national mathematics, science and technology education standards. SciMath<sup>MN</sup>'s mission is to increase the educational achievement and participation of all Minnesota students in science and mathematics to help them meet the complex challenges of their future.

*SciMath<sup>MN</sup> gratefully acknowledges the generous support of the Minnesota Legislature, the Minnesota Department of Education, Michigan State University (under the leadership of William H Schmidt) and the following Minnesota businesses and organizations in ensuring the 2007 TIMSS participation, as well as the 2008-2009 analysis and informational events.*



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